

Seminars on Formal Methods and Languages  
Inria Grenoble – Rhône-Alpes

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Grenoble, France

# Computing best and worst case execution time of real-time systems under uncertainty

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Joint work with Giuseppe Lipari, Sun Youcheng, Camille Coti, Nguyễn Hoàng Gia

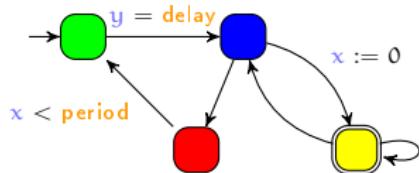


# Context: Critical systems

- Need for early bug detection
  - Bugs discovered when final testing: **expensive**  
~ Need for a thorough **modeling** and **verification** phase



# Timed model checking (1/2)

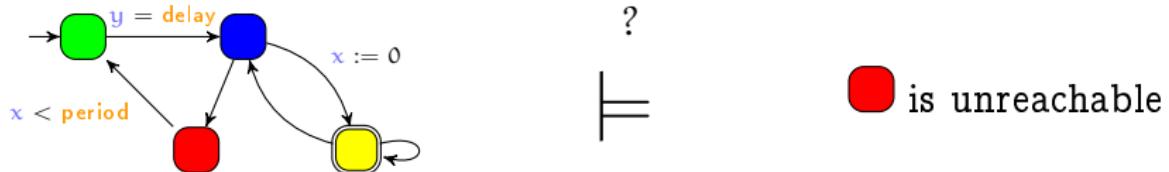


is unreachable

A **model** of the system

A **property** to be satisfied

# Timed model checking (1/2)

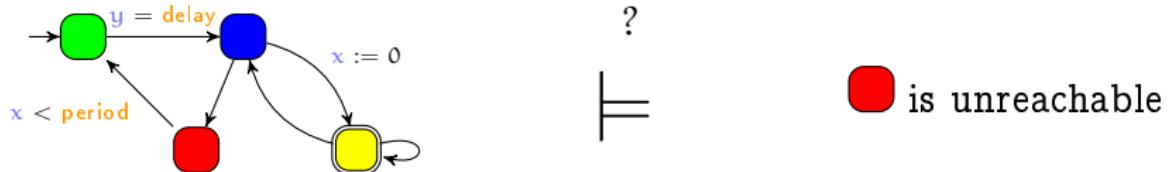


A **model** of the system

A **property** to be satisfied

- Question: does the model of the system satisfy the property?

# Timed model checking (1/2)



A **model** of the system

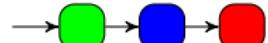
A **property** to be satisfied

- Question: does the model of the system satisfy the property?

**Yes**



**No**



Counterexample

# Timed model checking (2/2)

- Timed systems are characterized by a set of timing constants
  - “The packet transmission lasts for 50 ms”
  - “The sensor reads the value every 10 s”
- Powerful model checking tools, e.g.:
  - UPPAAL [Larsen et al., 1997]
  - PAT [Sun et al., 2009]

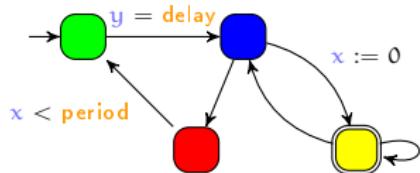
# Beyond timed model checking: parameter synthesis

- Verification for **one** set of constants does not usually guarantee the correctness for other values
- Challenges
  - **Numerous verifications:** is the system correct for any value within  $[40; 60]$ ?
  - **Optimization:** until what value can we increase 10?
  - **Robustness [Markey, 2011]:** What happens if 50 is implemented with 49.99?
  - **System incompletely specified:** Can I verify my system even if I don't know the period value with full certainty?

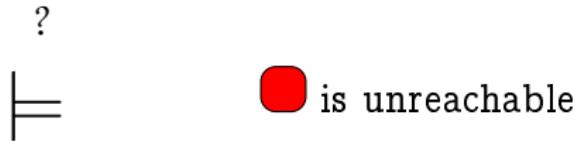
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- Parameter synthesis
  - Consider that timing constants are unknown constants (**parameters**)

# timed model checking



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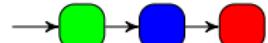
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Yes

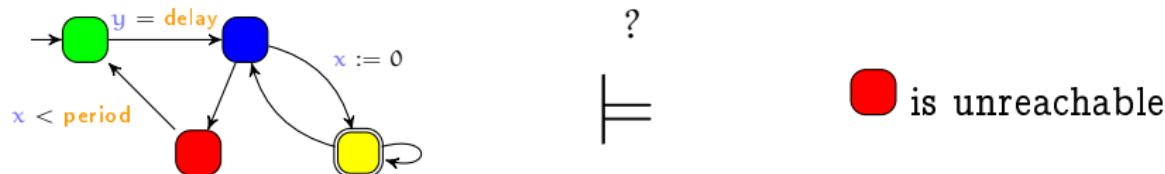


No



Counterexample

# Parametric timed model checking



A **model** of the system

A **property** to be satisfied

- Question: for what values of the parameters does the model of the system satisfy the property?

Yes if...



$$\begin{aligned} & 2\text{delay} > \text{period} \\ \wedge \quad & \text{period} < 20.46 \end{aligned}$$

# Outline

- 1 Parametric Timed Automata
- 2 Modeling and Verifying Real-Time Systems
- 3 Verifying a Real-time System under Uncertainty
- 4 Distributed Verification of Distributed Systems
- 5 Conclusion and Perspectives

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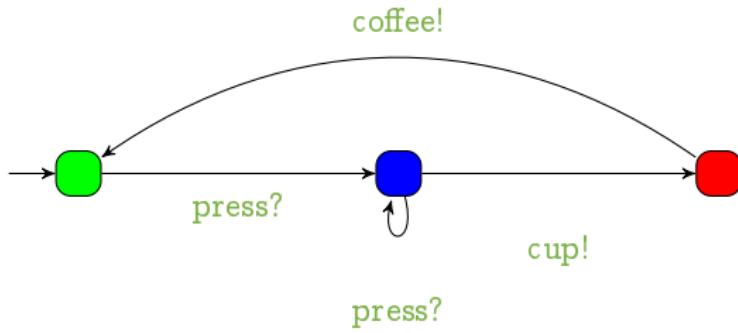
# Timed automaton (TA)

- Finite state automaton (sets of locations)



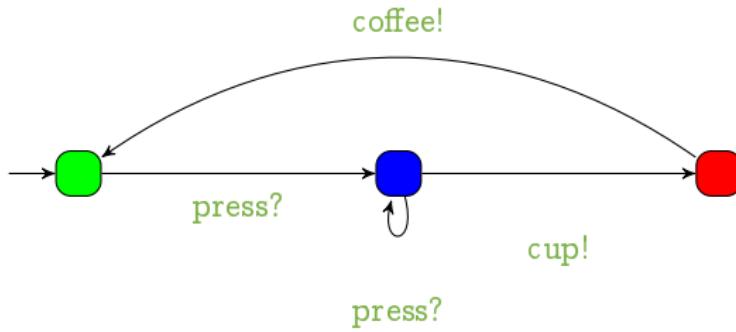
# Timed automaton (TA)

- Finite state automaton (sets of locations and actions)



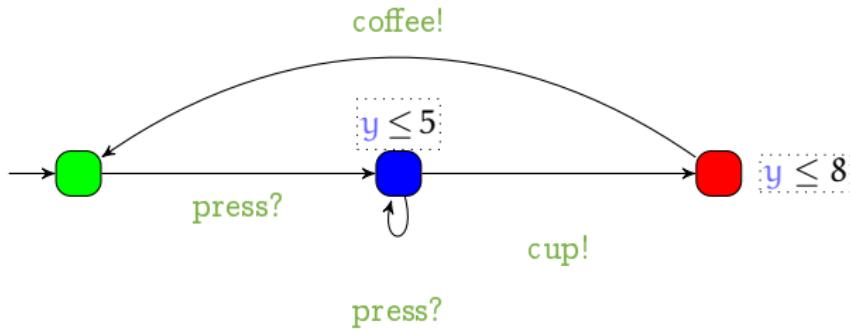
# Timed automaton (TA)

- Finite state automaton (sets of **locations** and **actions**) augmented with a set **X** of **clocks** [Alur and Dill, 1994, Henzinger et al., 1994]
  - Real-valued variables evolving linearly at the same rate



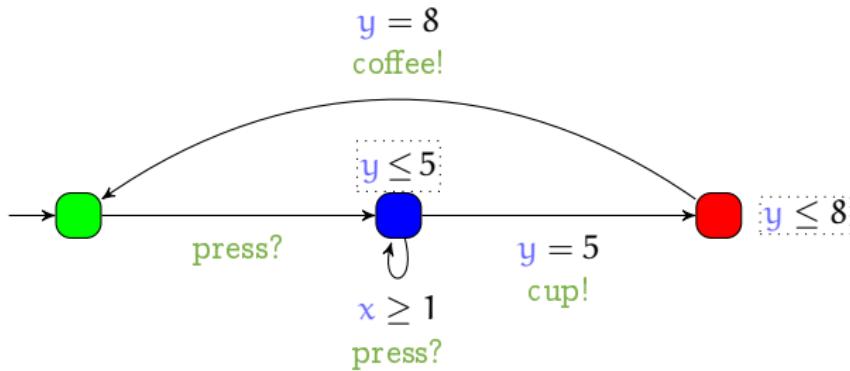
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  - Location **invariant**: constraint to be verified to stay at a location



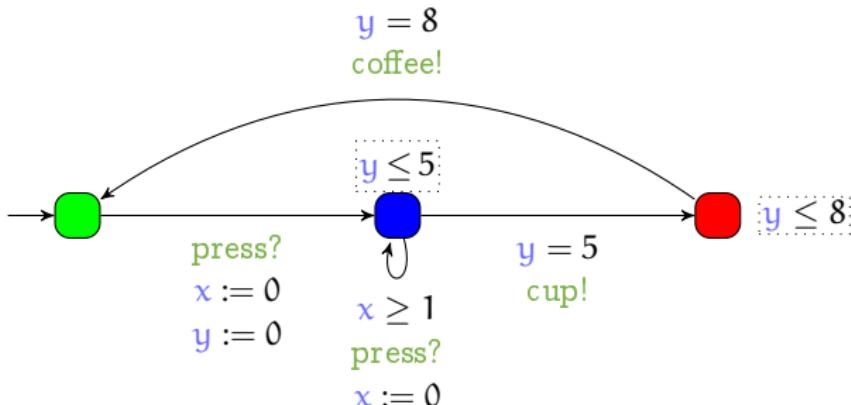
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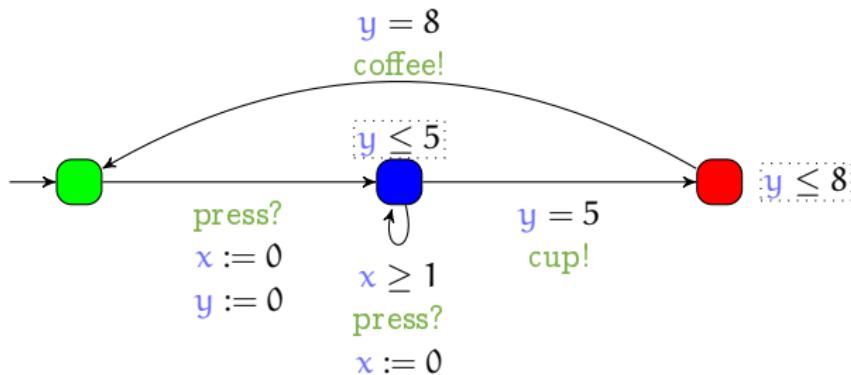
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- Features
  - Location **invariant**: constraint to be verified to stay at a location
  - Transition **guard**: constraint to be verified to enable a transition
  - Clock **reset**: some of the clocks can be set to 0 at each transition



# Concrete semantics of timed automata

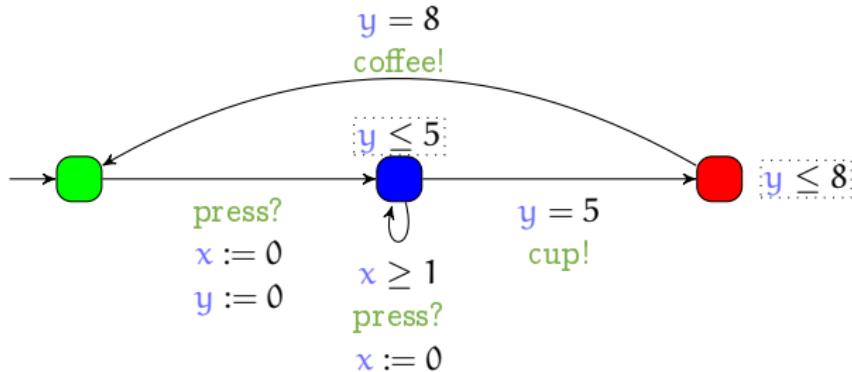
- Concrete state of a TA: pair  $(l, w)$ , where
  - $l$  is a location,
  - $w$  is a valuation of each clock
- Concrete run: alternating sequence of concrete states and actions or time elapse

## Examples of concrete runs



- Possible concrete runs for the coffee machine

# Examples of concrete runs



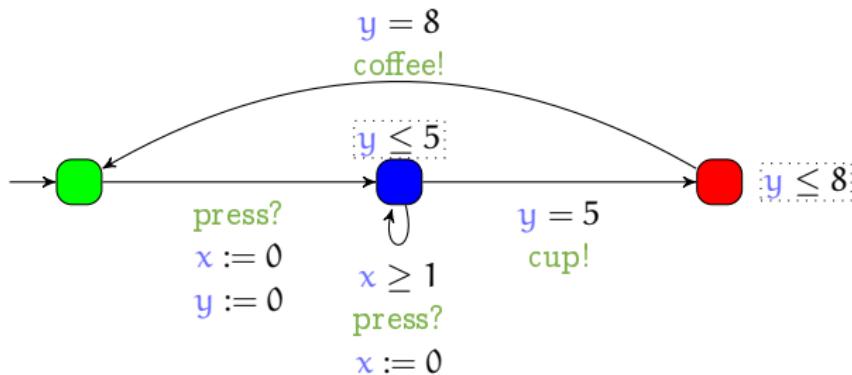
- Possible concrete runs for the coffee machine
  - Coffee with no sugar



$x$   
 $y$

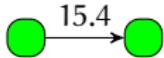
0  
0

# Examples of concrete runs



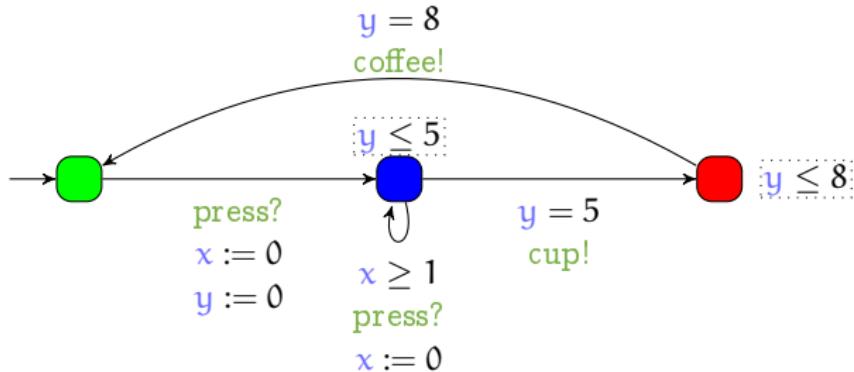
## ■ Possible concrete runs for the coffee machine

### ■ Coffee with no sugar



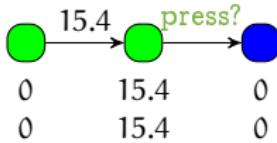
$x$	0	15.4
$y$	0	15.4

# Examples of concrete runs

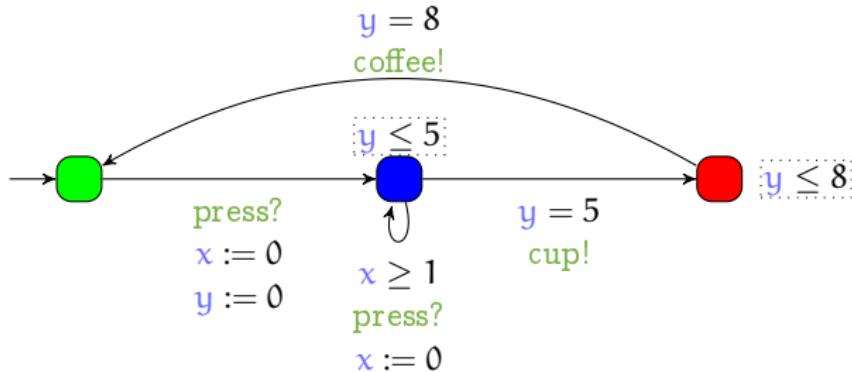


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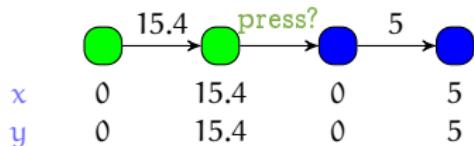


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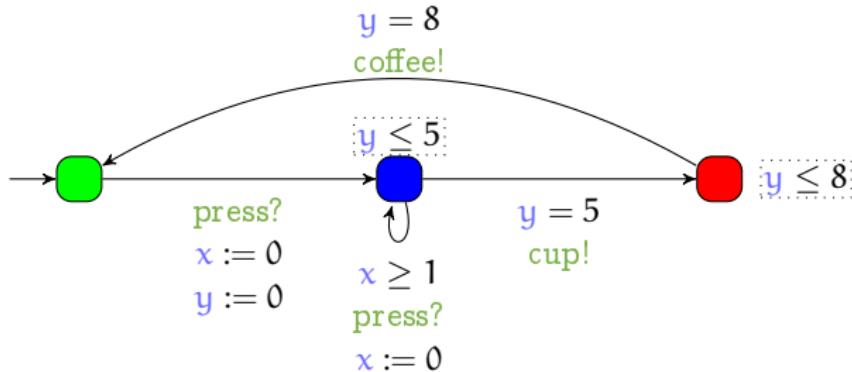


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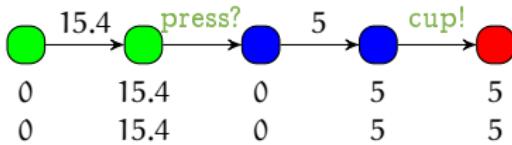


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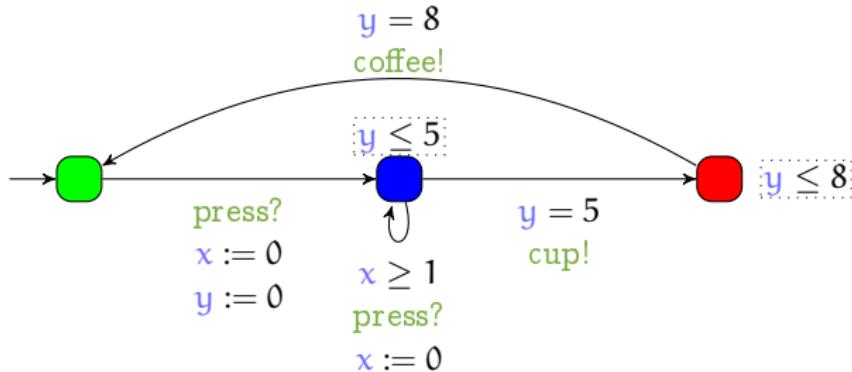


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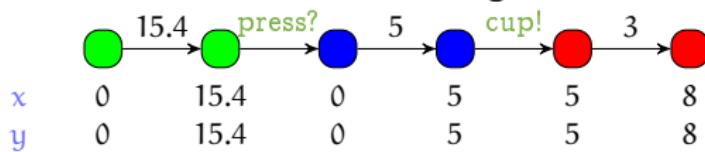


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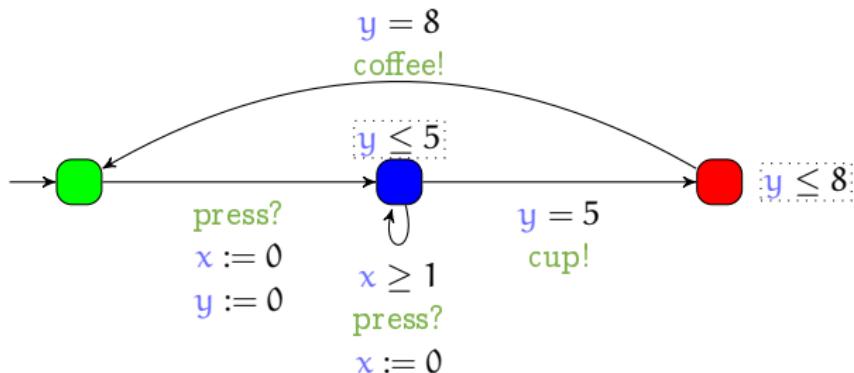


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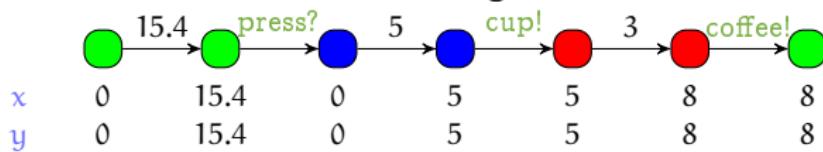


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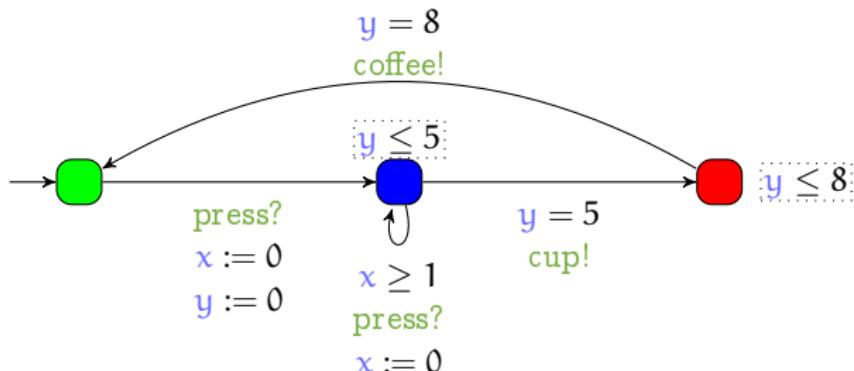


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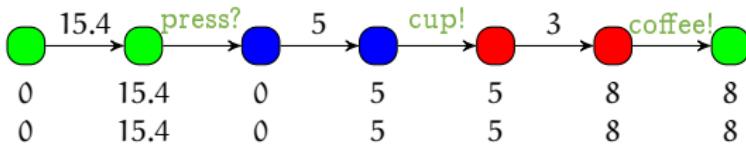


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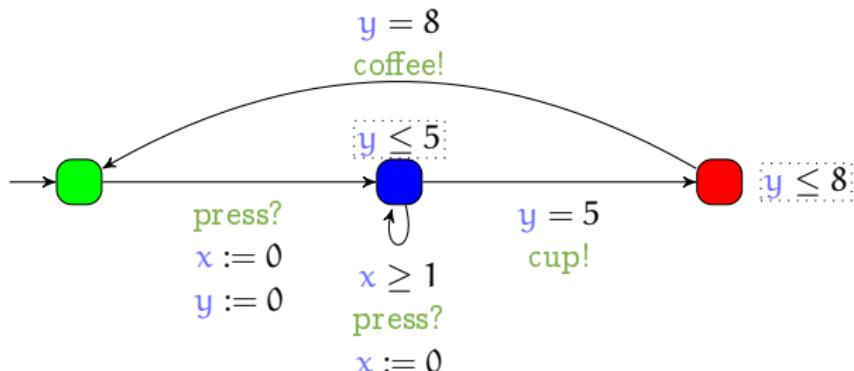


- Coffee with 2 doses of sugar



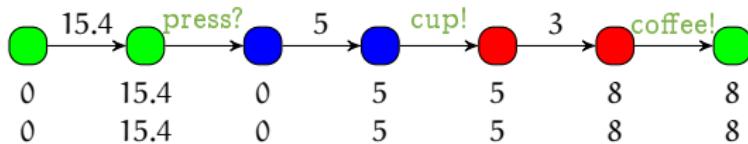
$x$   
0  
 $y$   
0

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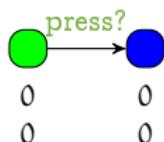


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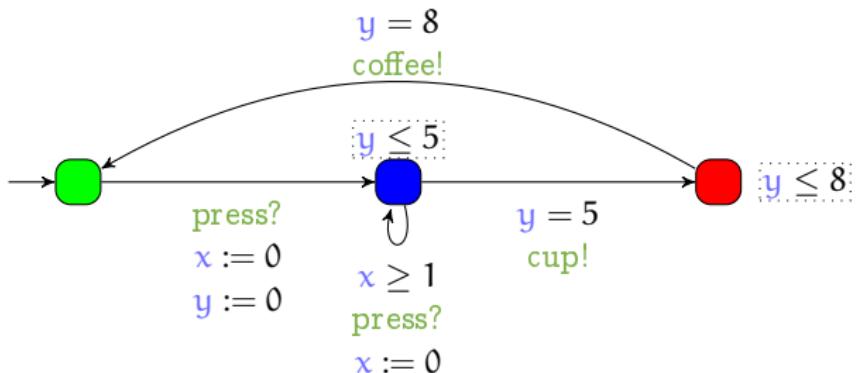
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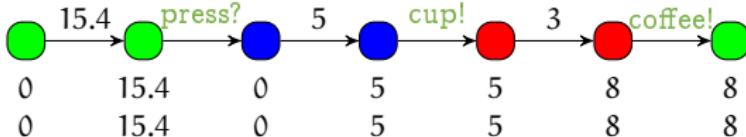


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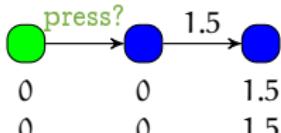


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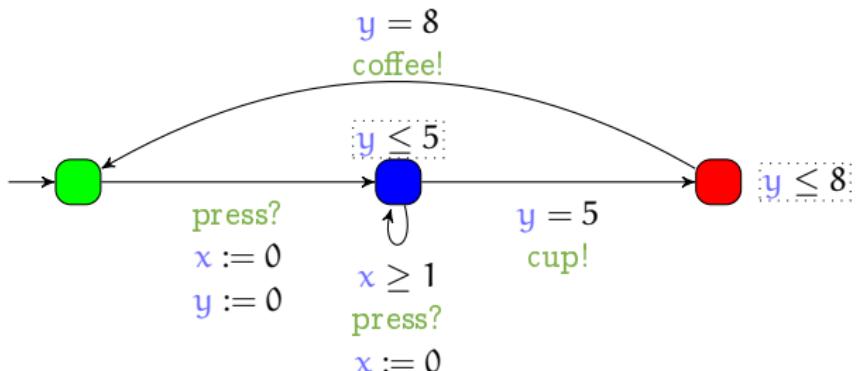
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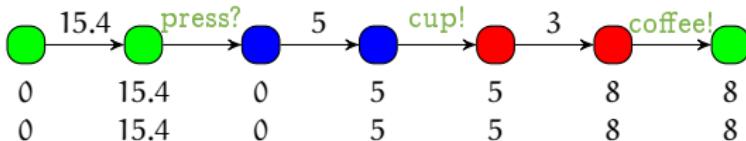


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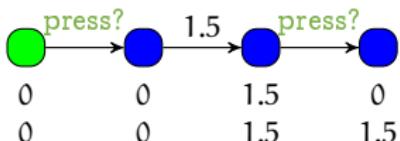


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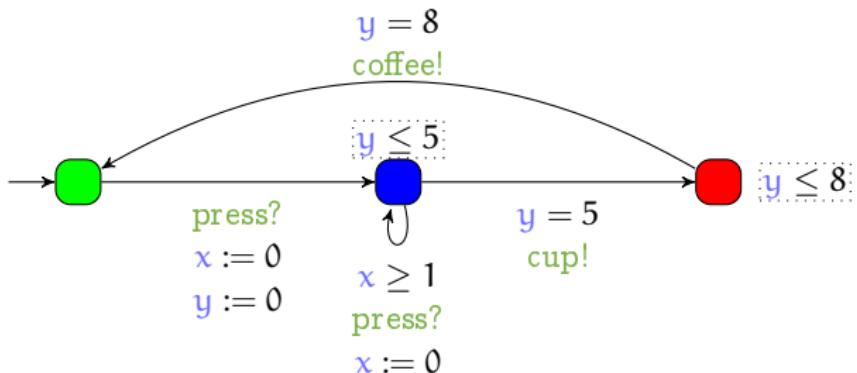
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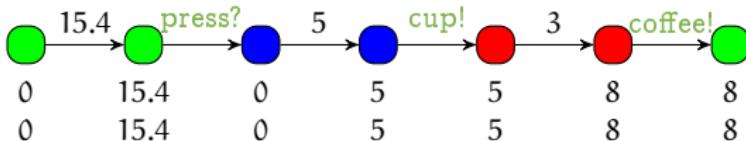


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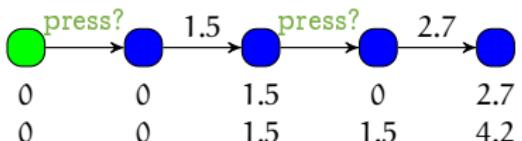


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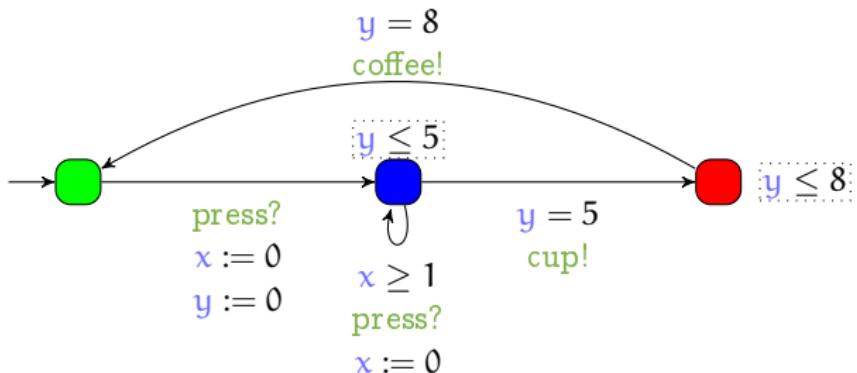
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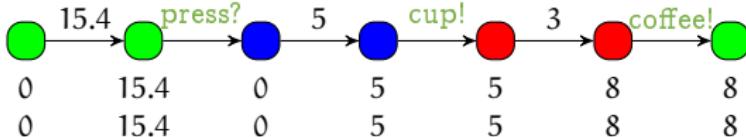


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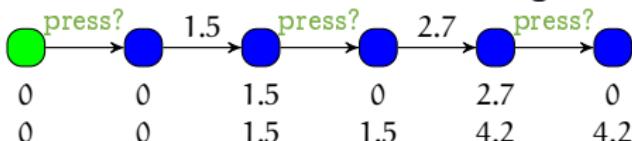


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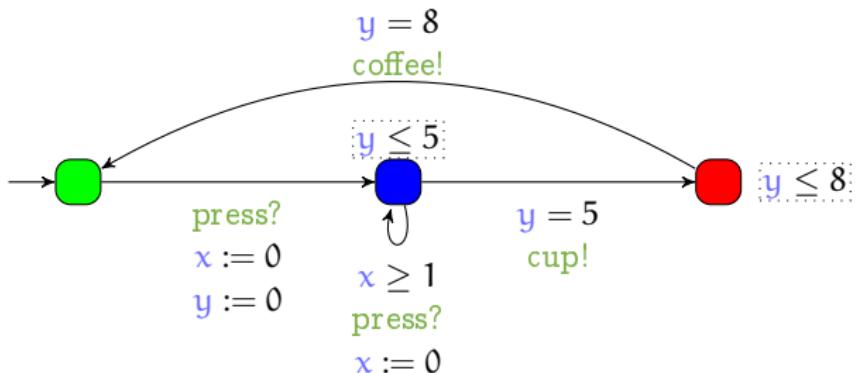
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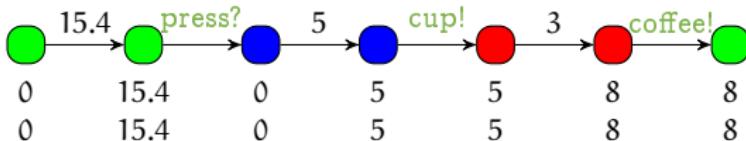


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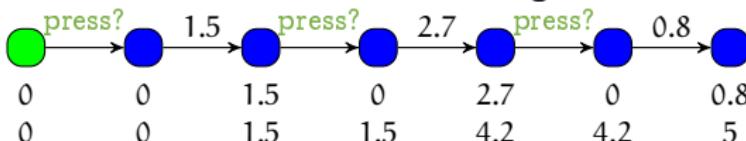


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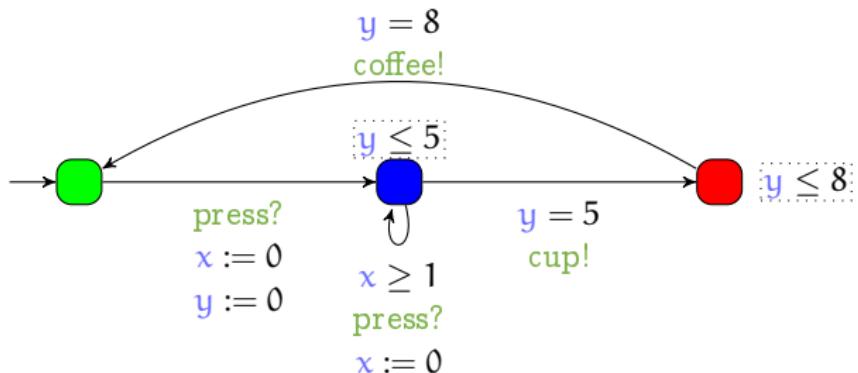
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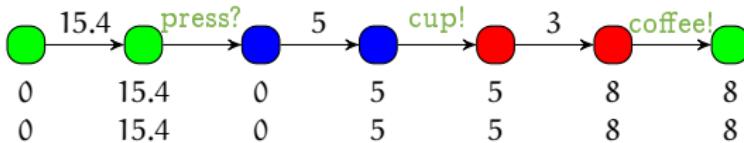


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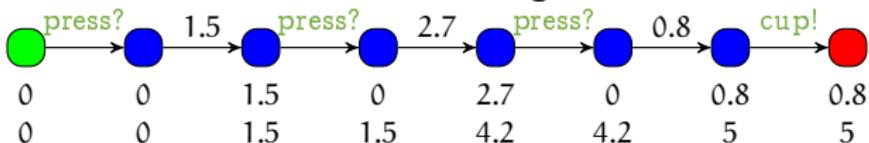


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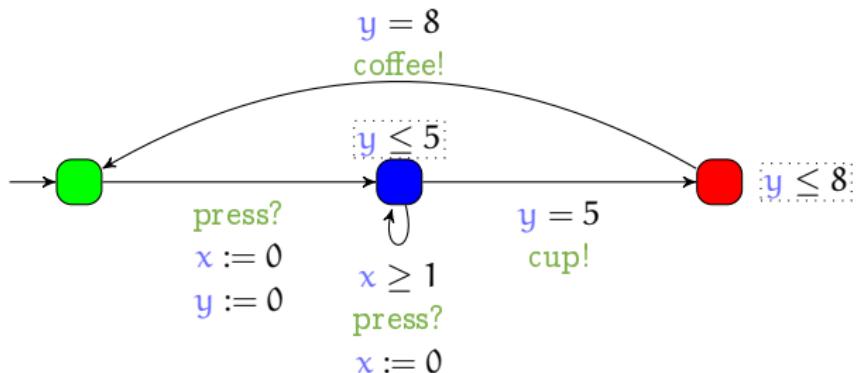
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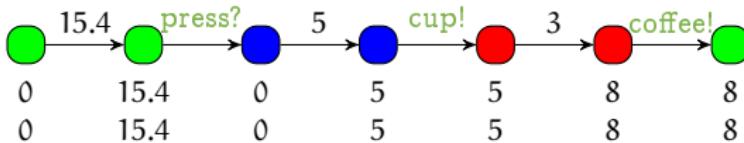


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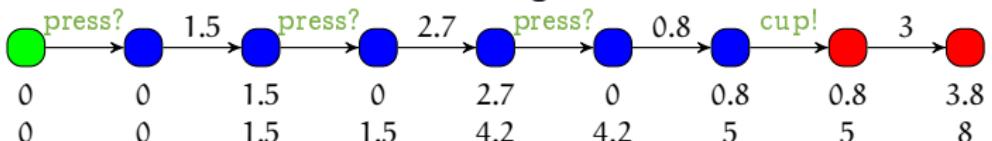


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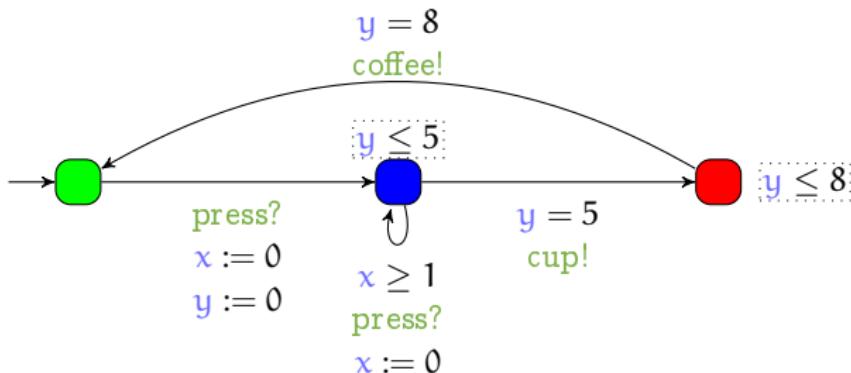
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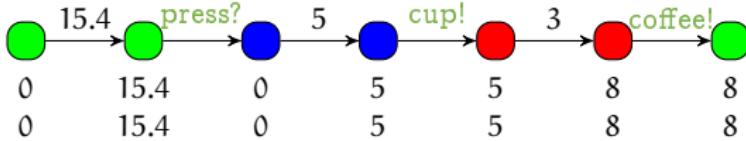


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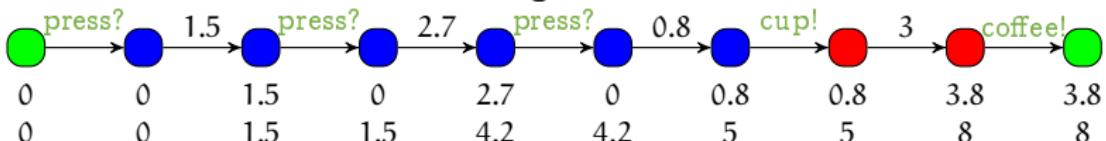


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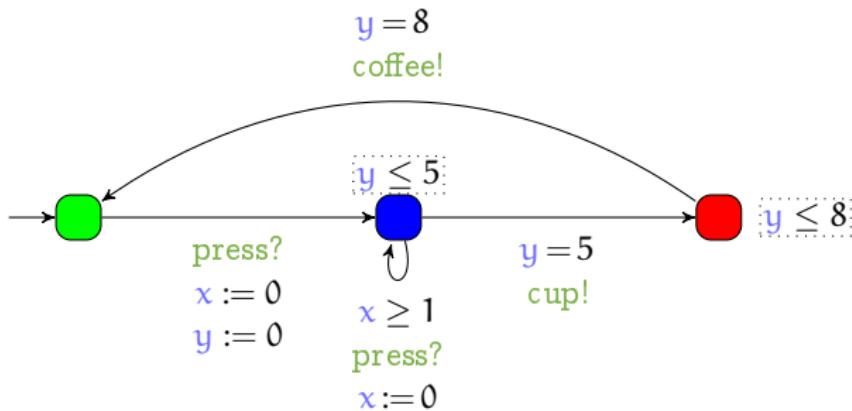


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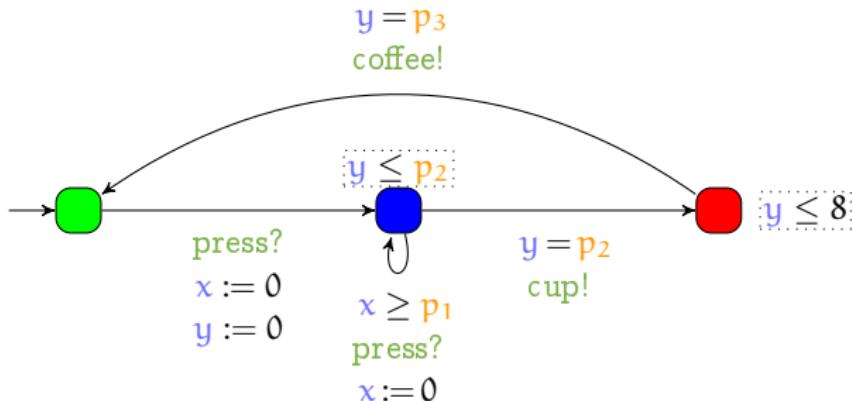
# Parametric timed automaton (PTA)

- Timed automaton (sets of locations, actions and clocks)



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- Timed automaton (sets of locations, actions and clocks)  
augmented with a set  $P$  of parameters [Alur et al., 1993]
  - Unknown constants used in guards and invariants



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## Context: Hard real-time embedded systems

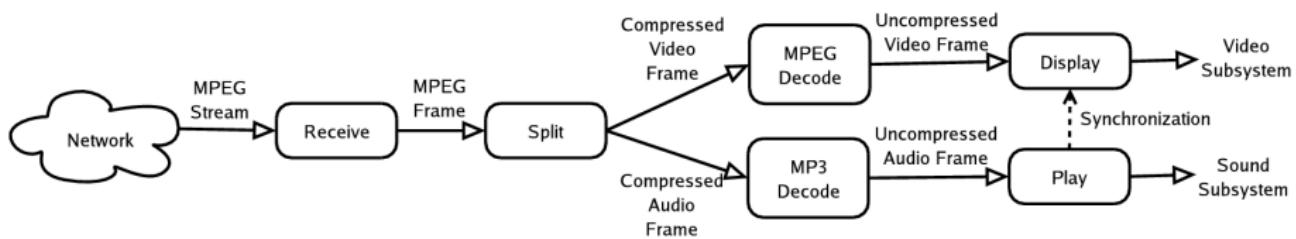
- Modern hard real-time embedded systems are **distributed** in nature
- Many of them have **critical timing requirements**:
  - **automotive systems** (modern cars have 10-20 embedded boards connected by one or more CAN bus)
  - **avionics systems** (several distributed control boards connected by one or more dedicated networks)



- To analyze the schedulability of such systems, it is very important to estimate the **(worst-case) computation times** of the tasks
- **Estimating WCET** is very difficult in modern architectures

# Real-time pipelines

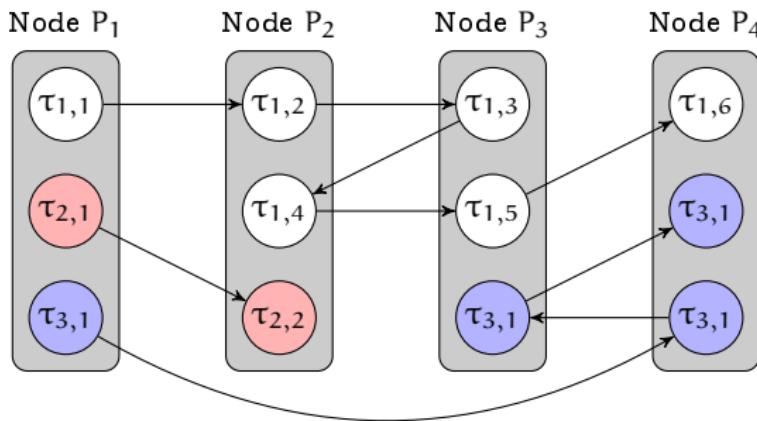
- Many real-time applications can be modeled as **pipelines** (also called **transactions**) of tasks



- Executed on a distributed (or multicore) system
- Activated cyclically (periodic or sporadic)

# Model

- A set of pipelines  $\{\mathcal{P}^{(1)}, \dots, \mathcal{P}^{(p)}\}$  distributed over  $m$  nodes
- Each pipeline  $\mathcal{P}^{(i)}$  is a chain of  $n_i$  tasks  $\{\tau_{i,1}, \dots, \tau_{i,n_i}\}$
- Pipeline  $\mathcal{P}^{(i)}$  has an end-to-end (E2E) deadline  $D_i$  and period  $T_i$

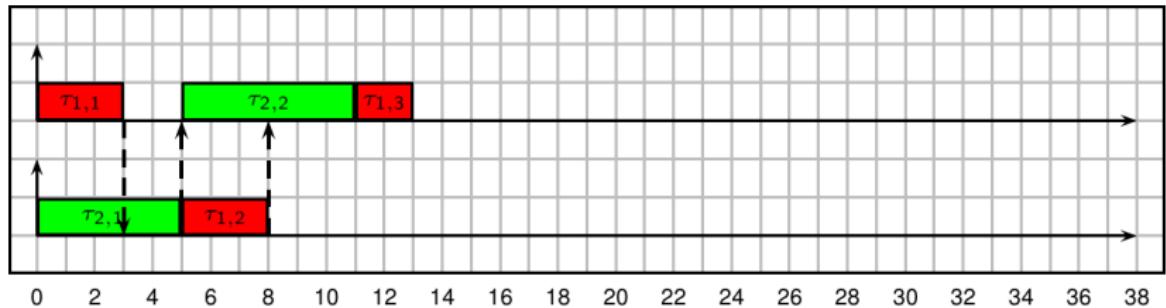
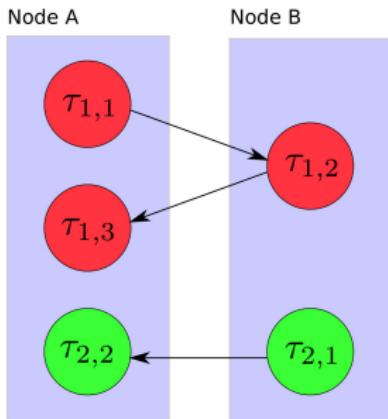


- Scheduling Problem: Guarantee that all pipelines complete before their E2E deadlines

# Activations, jitter, deadline

## ■ An example

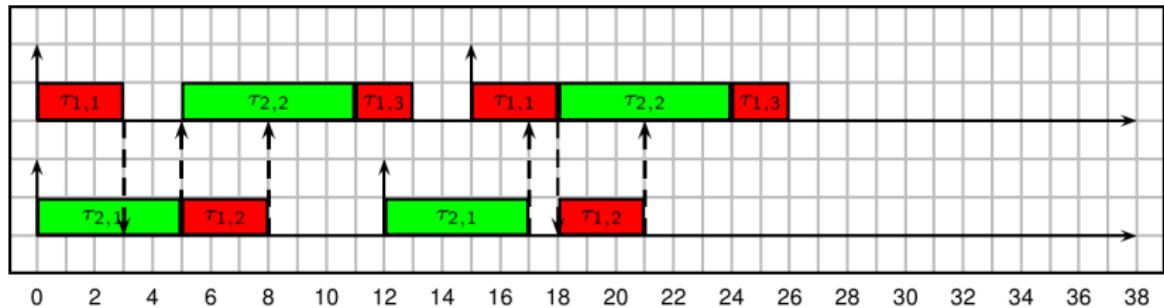
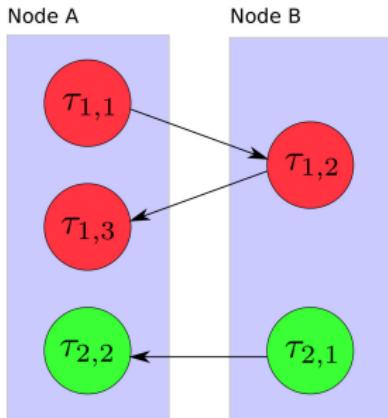
Task	Per.	E2E	Comp.	Resp.	Jitter	prio
$\tau_{1,1}$	15		3	3	0	HI
$\tau_{1,2}$	-		3	8	0-2	LO
$\tau_{1,3}$	-	15	2	13	3	LO
$\tau_{2,1}$	12		5	6	0	HI
$\tau_{2,2}$	-	12	6	?	0-1	ME



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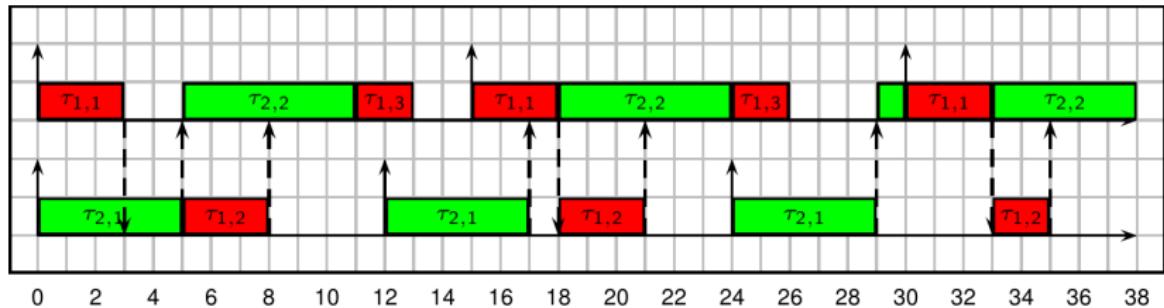
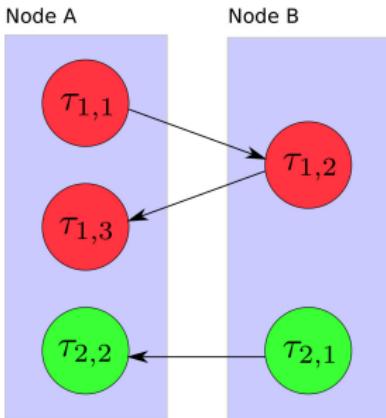
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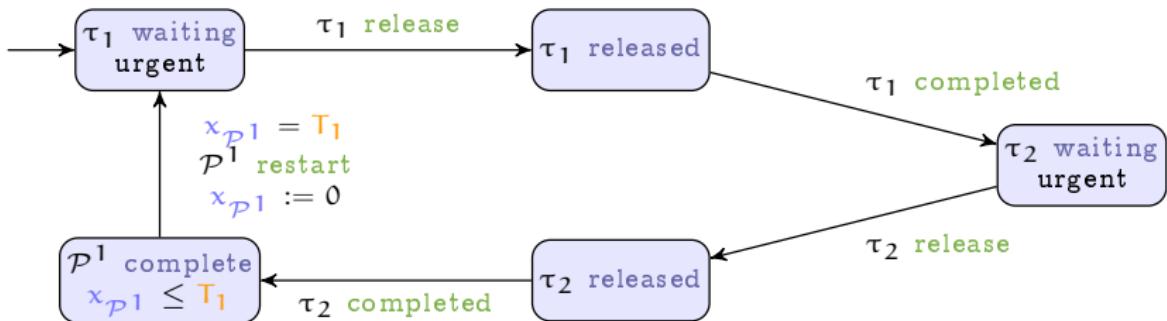
# Model of the network

- Tasks executing on processors are scheduled by Full Preemptive Fixed Priority Scheduler (FPFPS)
- Tasks send messages over the network to signal finishing of instance and activating the subsequent task
- Messages are scheduled over the network according to Non-Preemptive Fixed Priority
  - In the industrial domain, the CAN Bus features such a policy

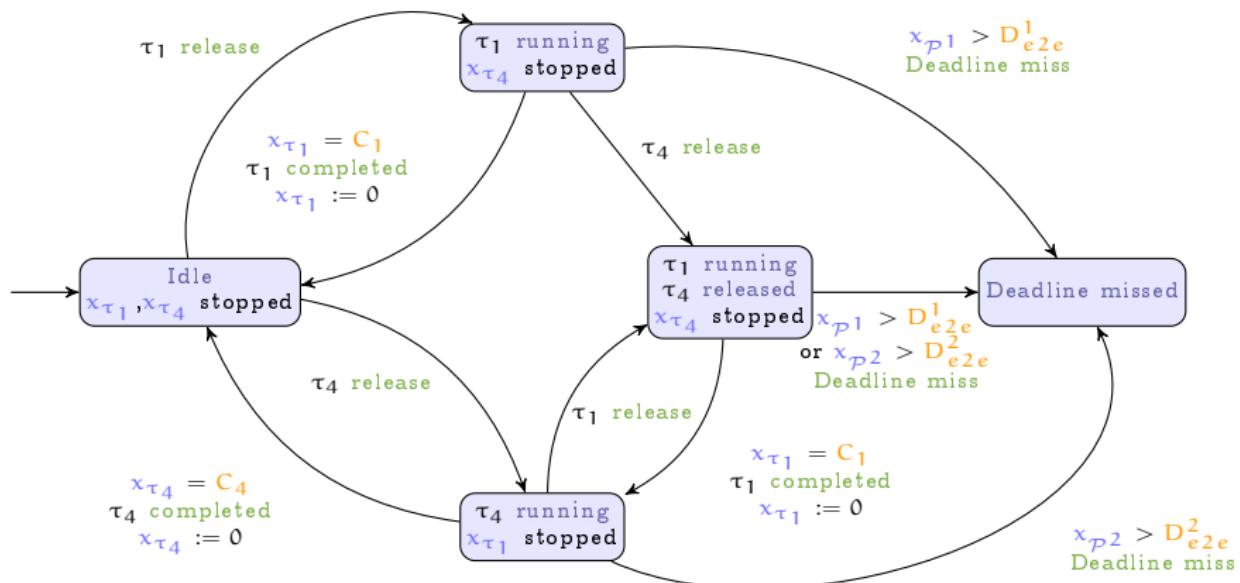
## Parametric model

- A task is identified by three parameters:
  - $C_i$  is the **worst-case computation time** (or worst-case transmission time, in case it models a message)
  - $R_i$  is the **task worst-case response time**, i.e., the worst case finishing time of any task instance relative to the activation of its pipeline.
  - $J_i$  is the task **worst-case activation jitter**, i.e., the greatest time since its activation that a task must wait for all preceding tasks to complete their execution
- The only one of interest is the **computation time**

# Modeling a task / pipeline



# Modeling the fixed priority scheduler (preemptive)



Actually a PTA extended with **stopwatches** [Sun et al., 2013]  
 an extension of stopwatch automata [Adbeddaïm and Maler, 2002]

# Parametric verification of real-time systems

Many problems can be reduced to parametric reachability (EFsynth):  
find parameter valuations for which a given state is unreachable

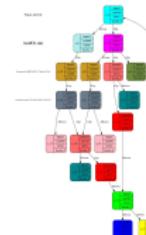
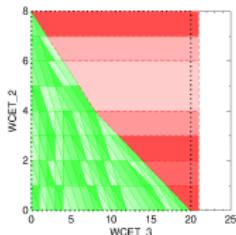
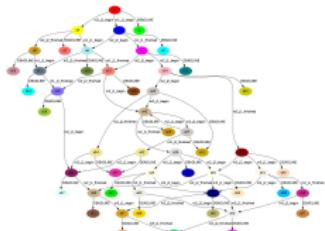
- ⌚ This problem is undecidable for PTAs and many subclasses  
[A., FTSCS 2015]
- ⌚ But we can still compute part (and often all) of the solution

Interesting problems:

- Find parameter valuations for which no deadline violation occurs (i. e., for which the system is schedulable)
- Compute the worst-case computation time
- Find the parametric WCET when the jitter is unknown

# IMITATOR

- A tool for modeling and verifying **real-time systems** with unknown constants modeled with **parametric timed automata**
  - Communication through (strong) broadcast synchronization
  - Integer-valued discrete variables
  - **Stopwatches**, to model schedulability problems with preemption
- Verification
  - Computation of the symbolic state space
  - Parametric model checking (using a subset of **TCTL**)
  - Language and trace preservation, and robustness analysis
  - Parametric deadlock-freeness checking
  - Behavioral cartography



# IMITATOR

Under continuous development since 2008

[André et al., 2012]

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- ... and more

Free and open source software: Available under the GNU-GPL license



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Try it!

[www.imitator.fr](http://www.imitator.fr)

## Some success stories

- Modeled and verified an asynchronous memory circuit by ST-Microelectronics
  - Project ANR Valmem
- Parametric schedulability analysis of a prospective architecture for the flight control system of the next generation of spacecrafts designed at ASTRIUM Space Transportation [Fribourg et al., 2012]
- Formal timing analysis of music scores [Fanchon and Jacquemard, 2013]
- Solution to a challenge related to a distributed video processing system by Thales

# Outline

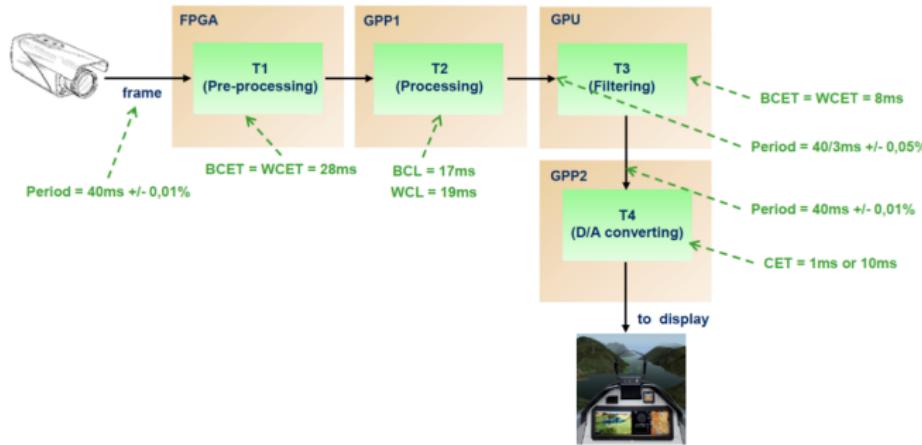
- 1 Parametric Timed Automata
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- 3 Verifying a Real-time System under Uncertainty
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# The FMTV 2015 Challenge (1/2)

Challenge by Thales proposed during the WATERS 2014 workshop  
Solutions presented at WATERS 2015

System: an unmanned aerial video system with **uncertain periods**

- Period constant but with a small uncertainty (typically 0.01 %)
- Not a jitter!



# The FMTV 2015 Challenge (2/2)

## Goal

Compute the end-to-end BCET and WCET times for a buffer size of  $n = 1$  and  $n = 3$

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  - No parameters in the specification

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Compute the end-to-end BCET and WCET times for a buffer size of  $n = 1$  and  $n = 3$

⌚ Not a typical parameter synthesis problem?

- No parameters in the specification

⌚ A typical parameter synthesis problem

- The end-to-end time can be set as a **parameter**... to be synthesized
- The uncertain period is typically a **parameter** (with some constraint, e. g.,  $P1 \in [40 - 0.004, 40 + 0.004]$ )

# Methodology

- 1 Propose a PTA model with **parameters** for uncertain periods and the end-to-end time

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Note: not eliminating parameters allows one to know for **which values of the periods** the best / worst case execution times are obtained.

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- 6 Exhibit the minimum and the maximum

Note: not eliminating parameters allows one to know for **which values of the periods** the best / worst case execution times are obtained.

# To build the PTA model

- Uncertainties in the system:

- $P1 \in [40 - 0.004, 40 + 0.004]$
- $P3 \in [\frac{40}{3} - \frac{1}{150}, \frac{40}{3} + \frac{1}{150}]$
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- Parameters:

- $P1\_uncertain$
- $P3\_uncertain$
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- Parameters:
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  - $P3\_uncertain$
  - $P4\_uncertain$
- The end-to-end latency (another parameter):  $E2E$
- Others:
  - the register between task 2 and task 3: discrete variable  $reg_{2,3}$
  - the buffer between task 3 and task 4:  $n = 1$  or  $n = 3$

# Simplification

- T1 and T2 are synchronised; T1, T3 and T4 are asynchronous
  - (exact modeling of the system behaviour is too heavy)

# Simplification

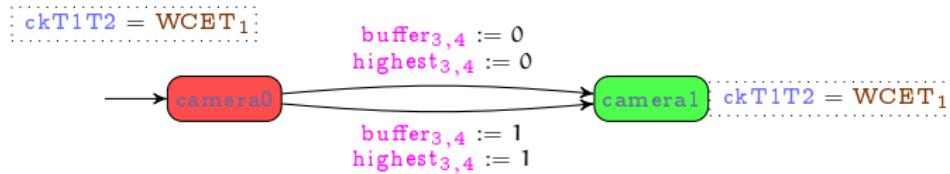
- T1 and T2 are synchronised; T1, T3 and T4 are asynchronous
  - (exact modeling of the system behaviour is too heavy)
- We choose a single arbitrary frame, called the **target** one
- We assume the system is initially in an arbitrary status
  - This is our only uncertain assumption (in other words, can the periods deviate from each other so as to yield any arbitrary deviation?)

# The initialization automaton

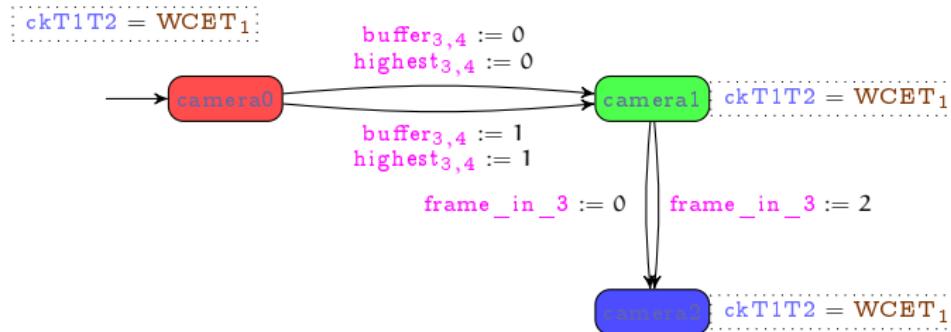
$\text{ckT1T2} = \text{WCET}_1$



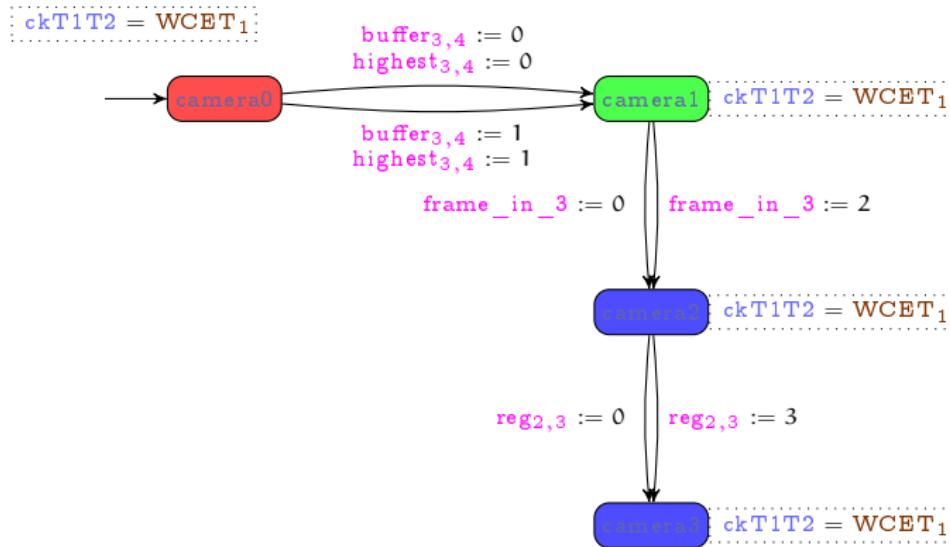
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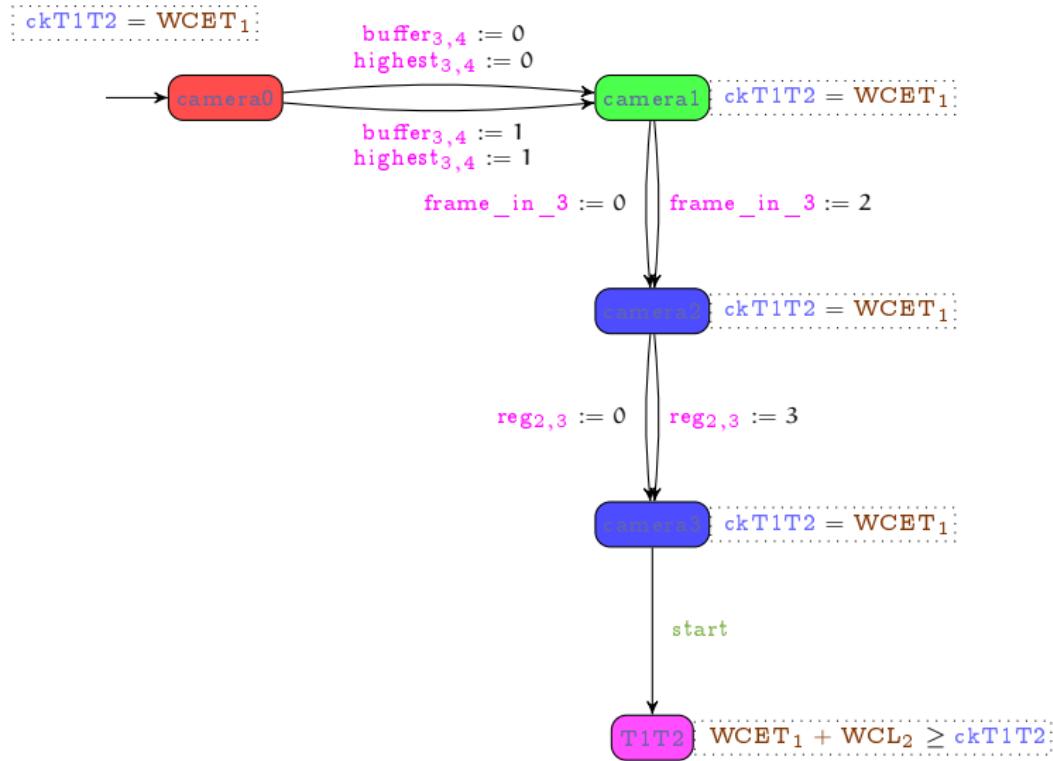
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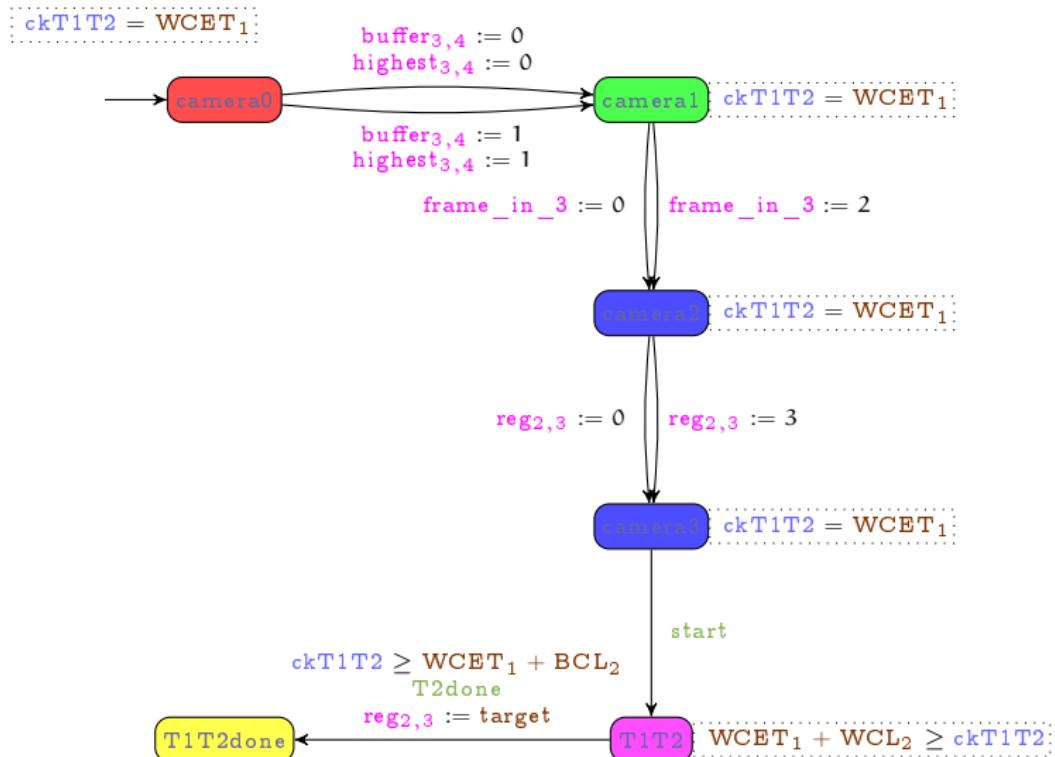
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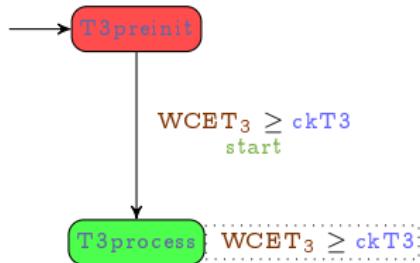
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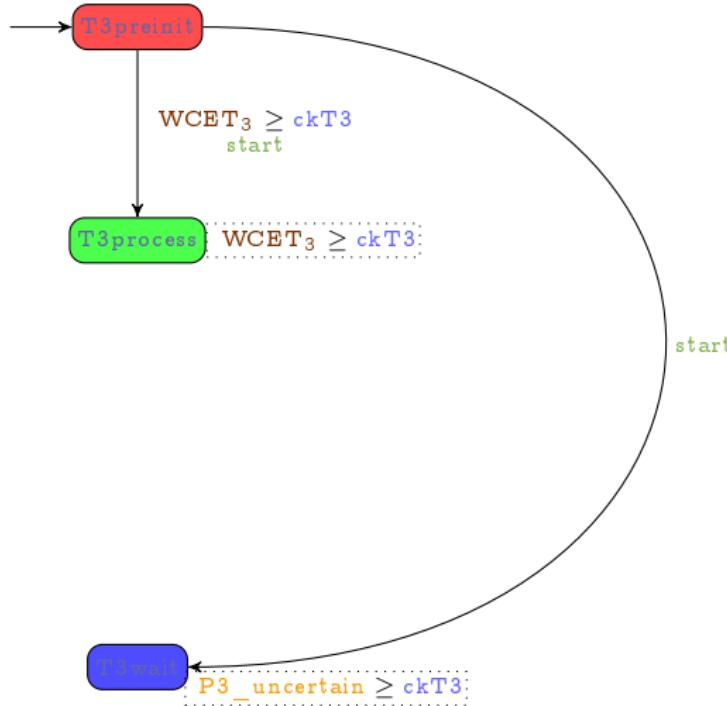
# Task T3



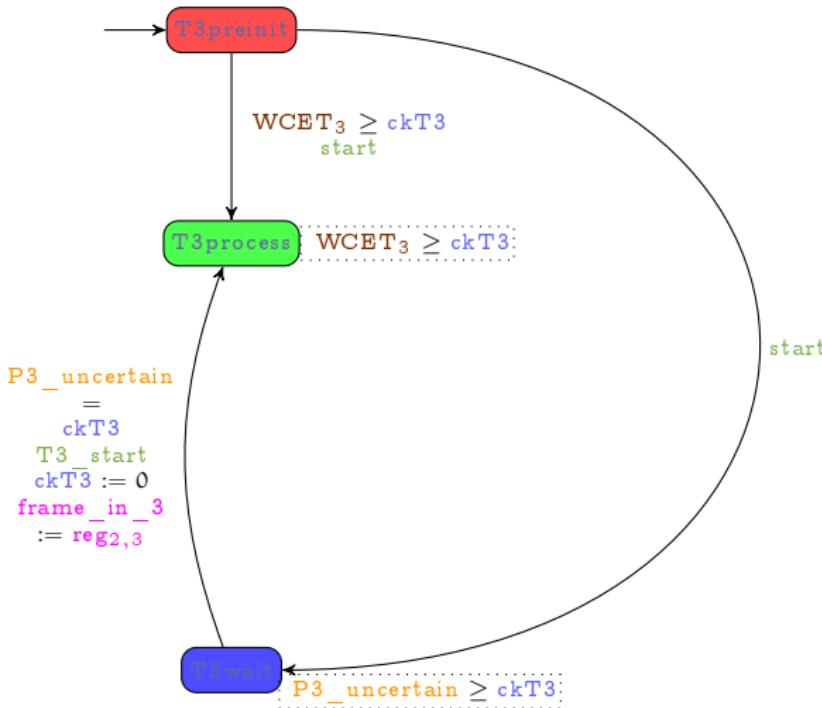
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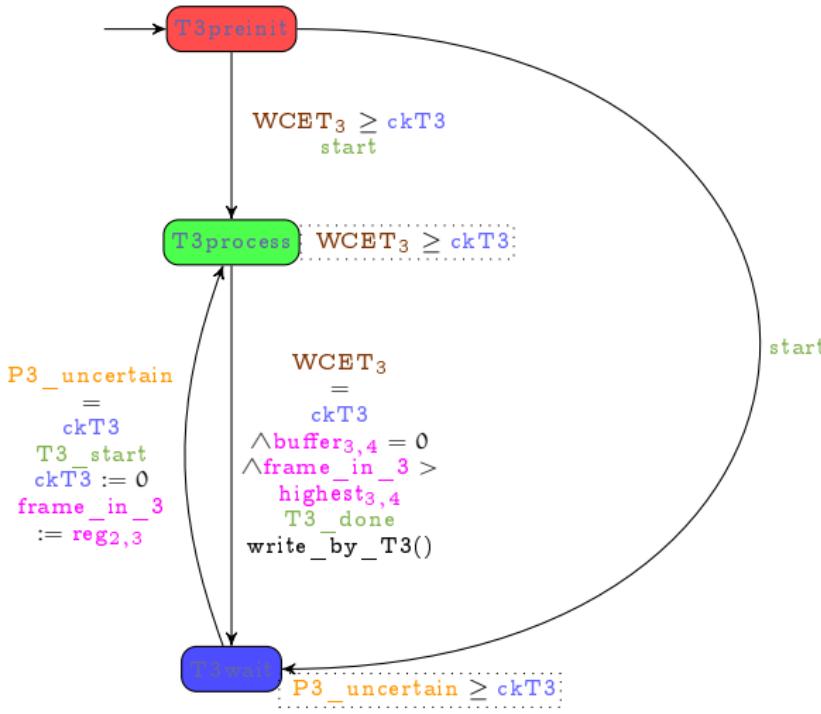
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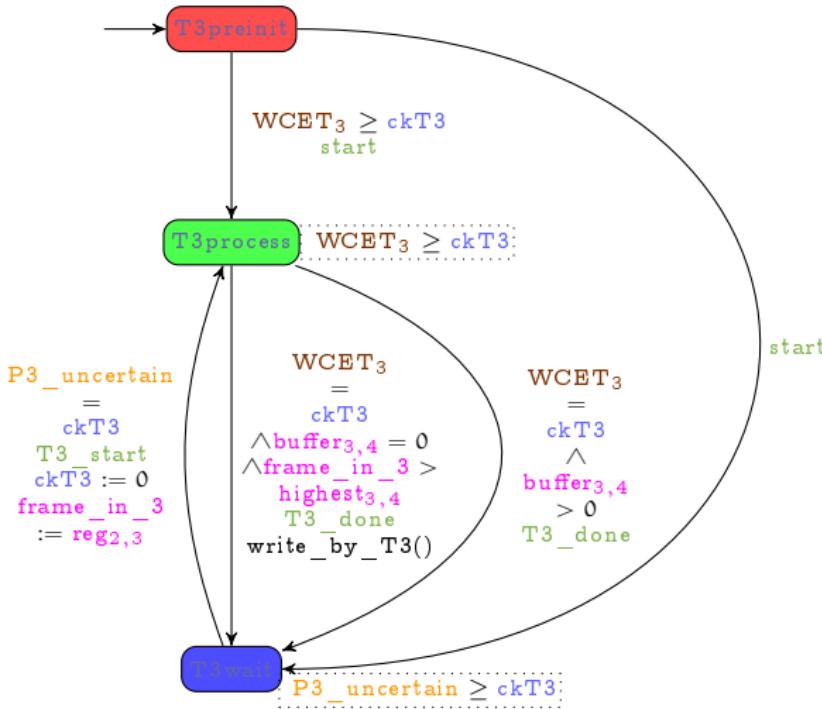
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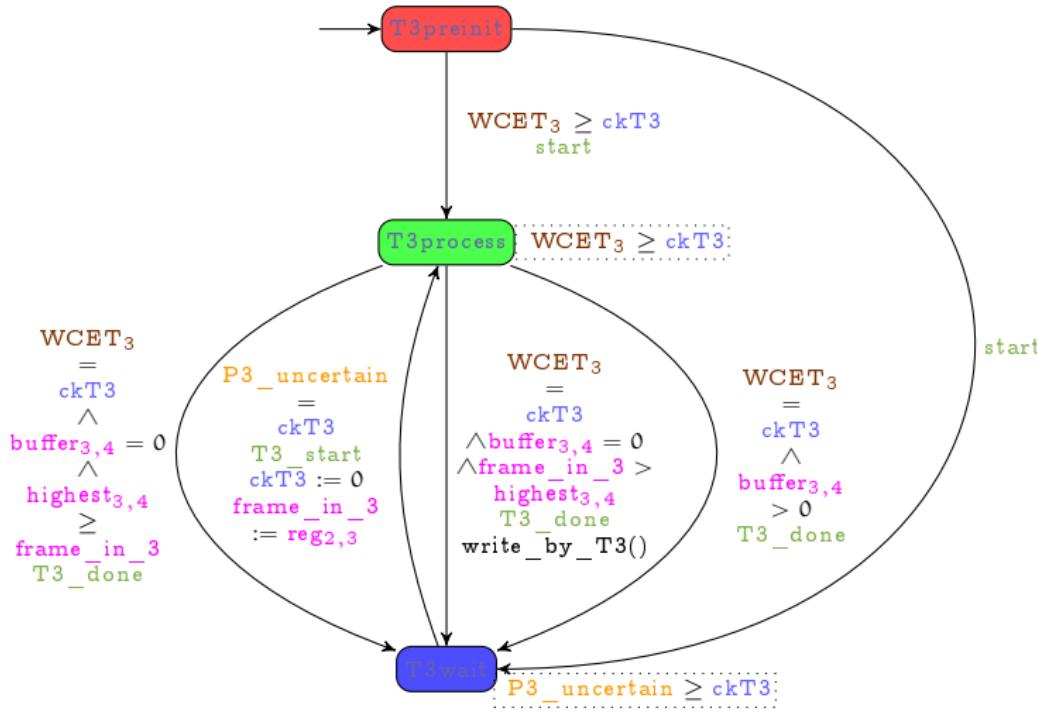
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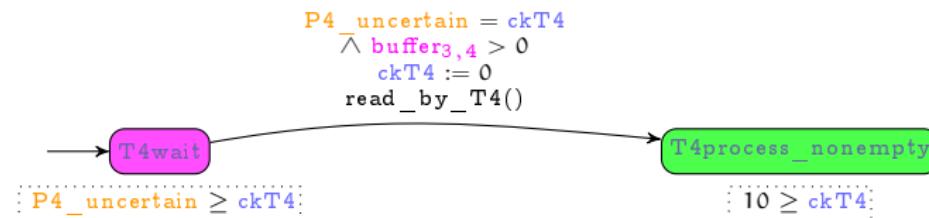


# Task T4

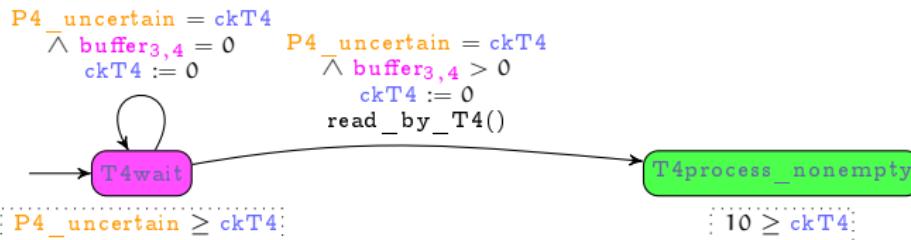


P4\_uncertain  $\geq$  ckT4;

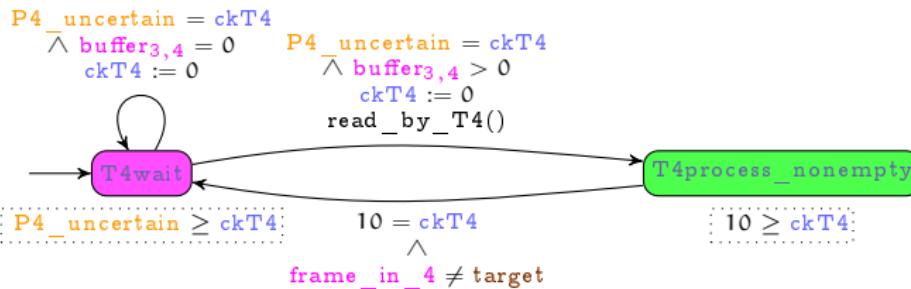
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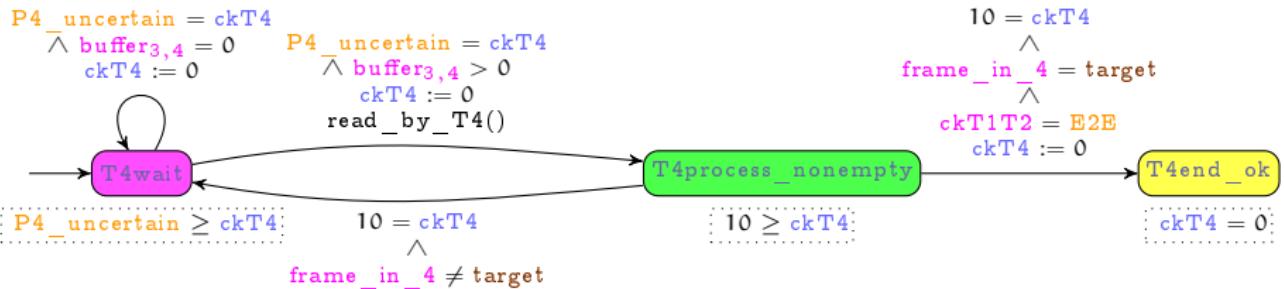
## Task T4



# Task T4



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# Results

E2E latency results for  $n = 1$  and  $n = 3$

	$n = 1$	$n = 3$
min E2E	63 ms	63 ms
max E2E	145.008 ms	225.016 ms

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# Why distributed algorithms?

Algorithms for parameter synthesis for PTA are very **costly**

- time
- memory

Some reasons:

- expensive operations on polyhedra
  - In IMITATOR: PPL [Bagnara et al., 2008]
- no known efficient data structure (such as BDDs or DBMs for timed automata)

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Idea: benefit from the power of **clusters**

- Cluster: large set of **nodes** (computers with their own memory and processor)
- Communication between nodes over a network

## A first naive approach

Naive approach to distribute EFsynth:

- Each node handles a subpart of the parameter domain
- Each node launches EFsynth on its parameter domain

Drawback: bad performances if the analysis is much more costly in some subdomains than in others

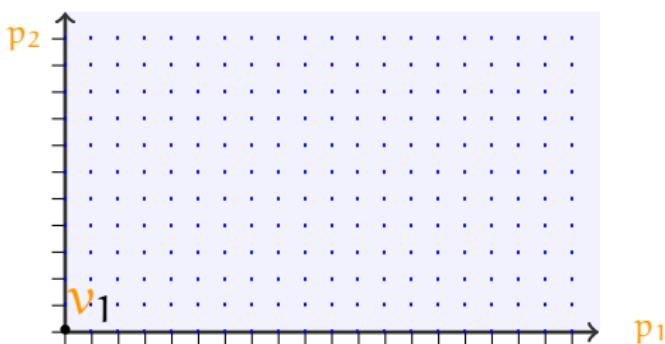
# A more elaborate master-worker approach

**Workers:** run a “hybrid” algorithm

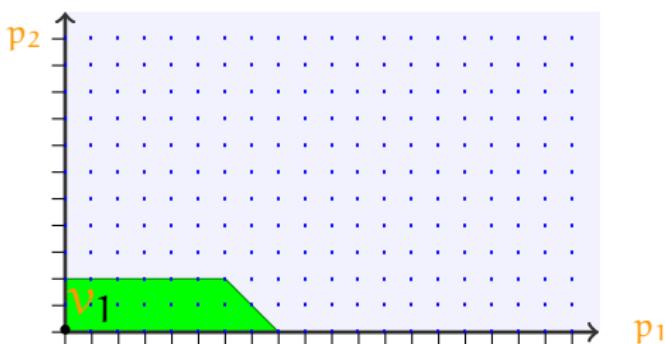
- PRP: parametric reachability preservation
- based on (integer) points: generalizes the reachability of the bad state as in the reference valuation (point)
- inspired by both EFsynth (to look for bad valuations) and TPsynth (to only explore a limited part of the symbolic state space, while “imitating” a reference valuation)
- guarantees the coverage of all integer points (but rational-valued points may be missing)

**Master:** responsible for gathering results and distributing reference valuations (“points”) among workers

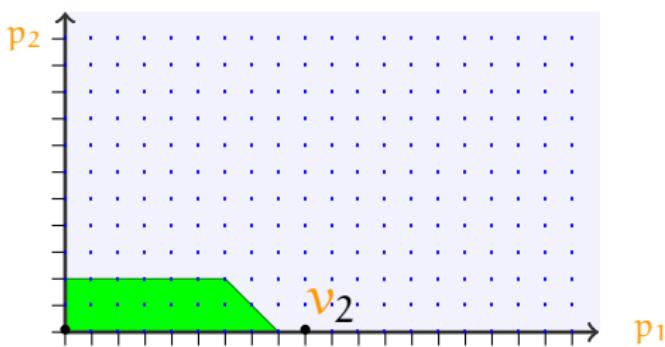
# Parametric reachability preservation cartography (PRPC)



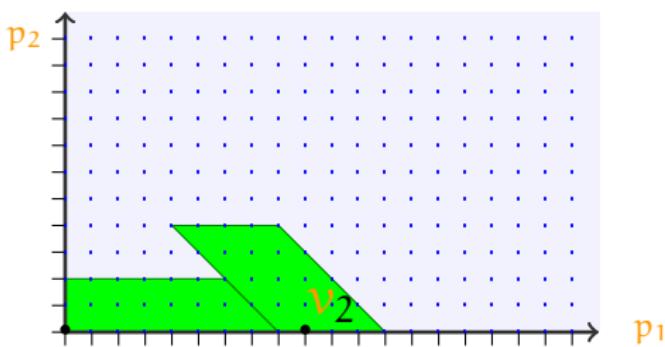
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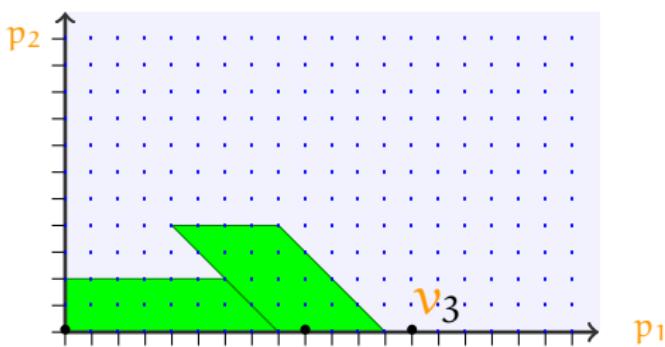
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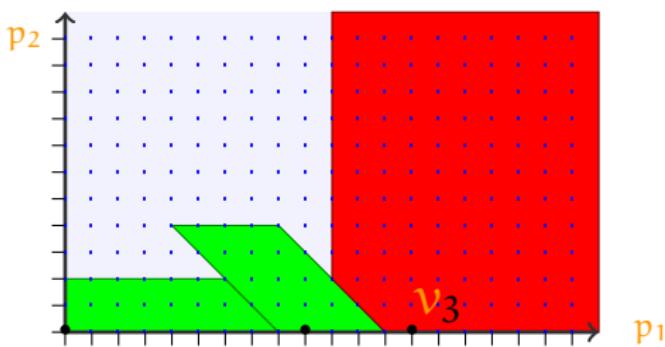
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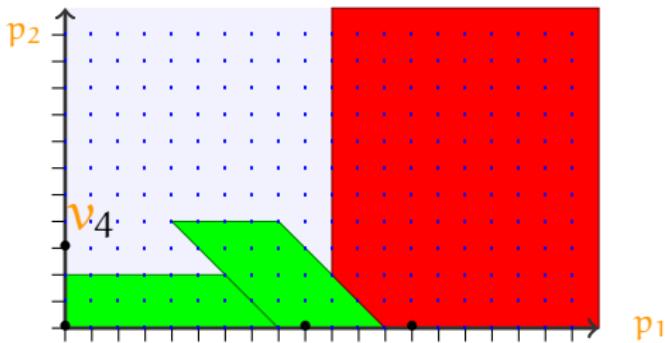
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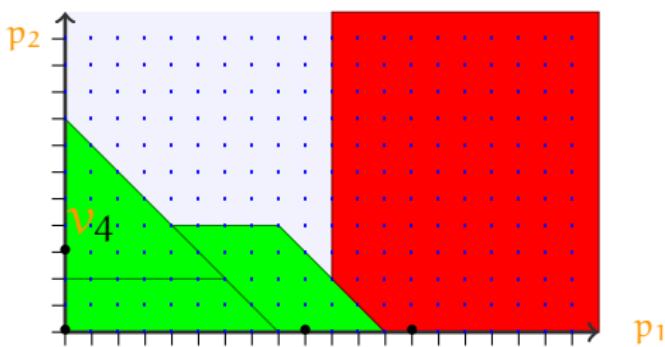
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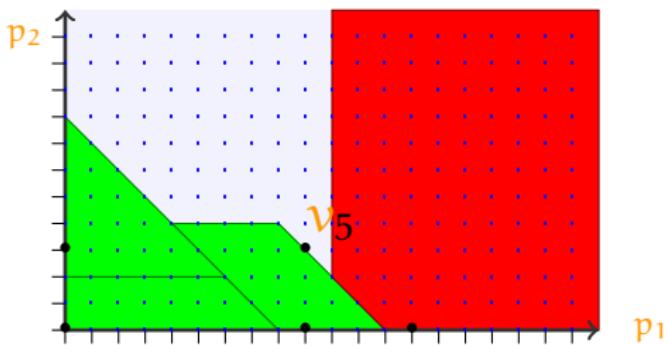
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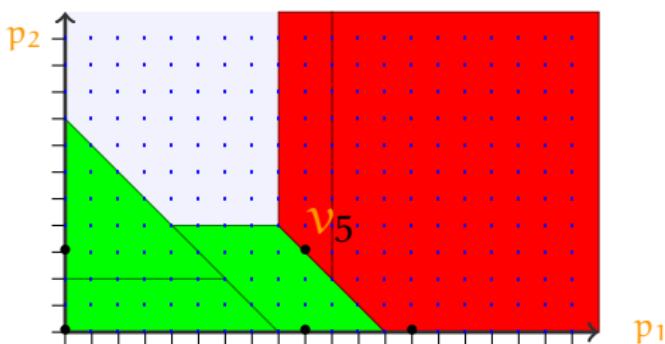
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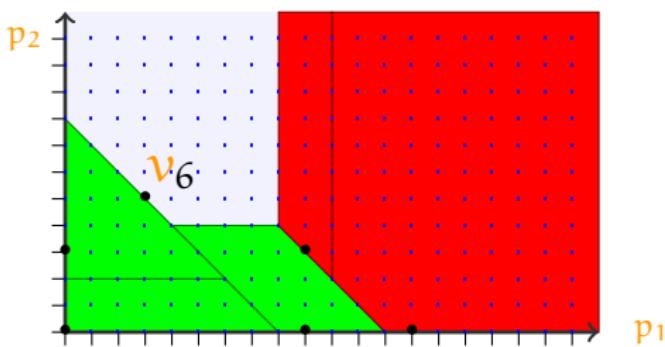
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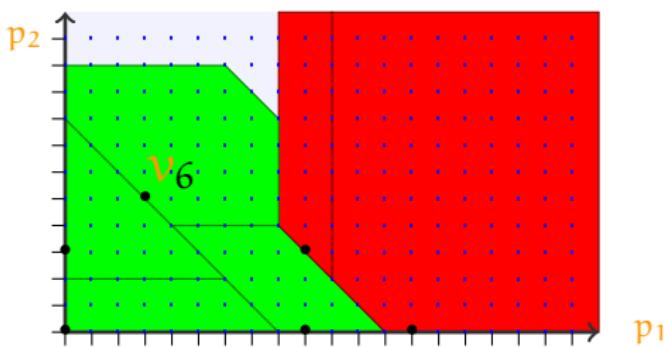
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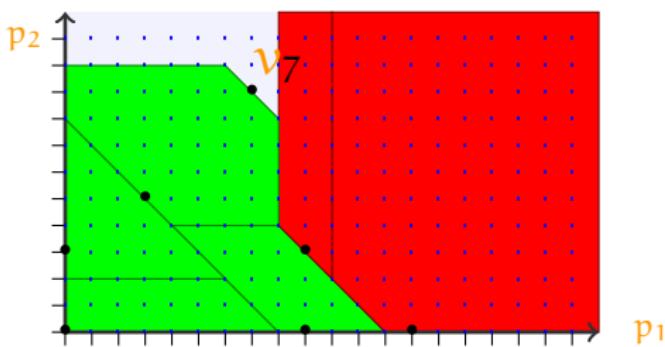
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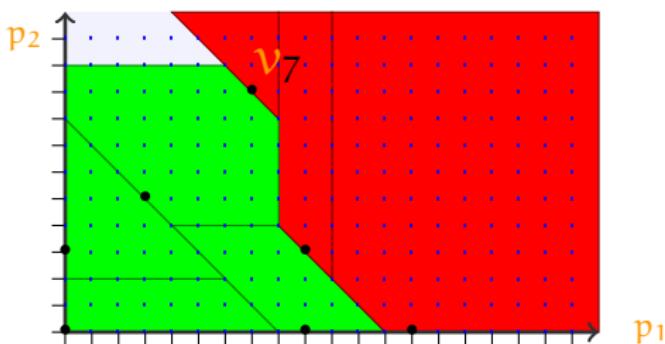
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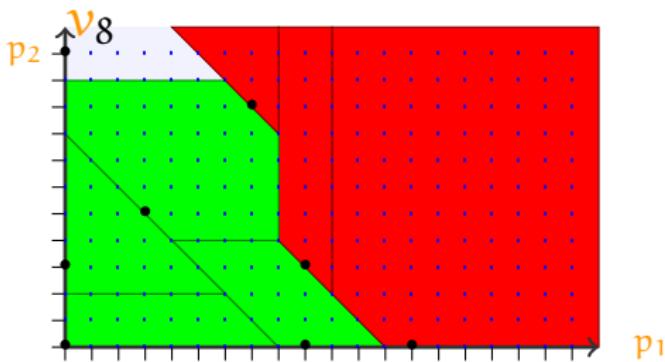
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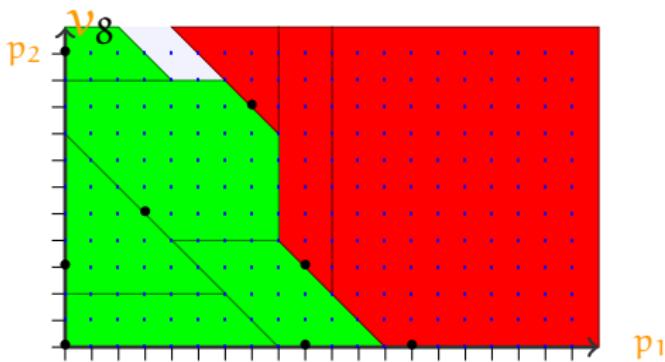
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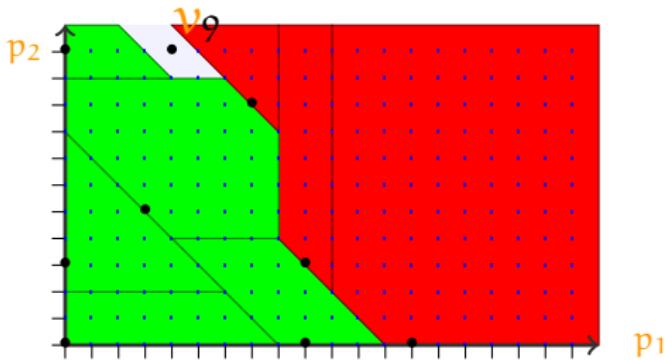
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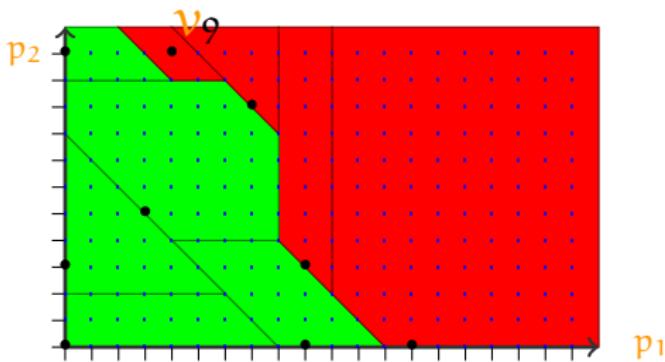
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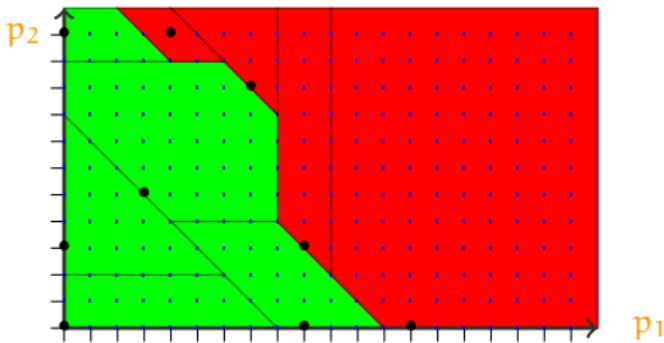
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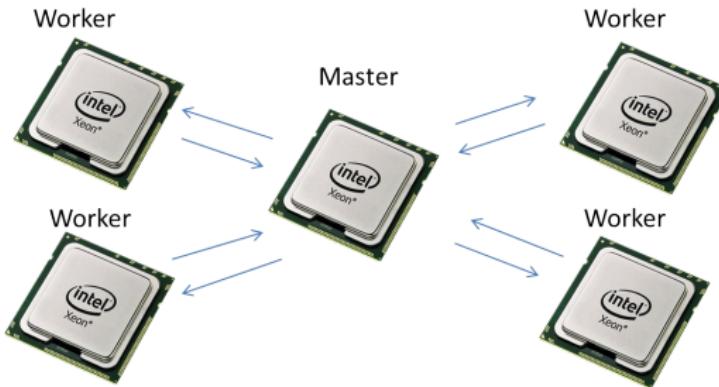
# Parametric reachability preservation cartography (PRPC)



# Parametric reachability preservation cartography (PRPC)



# Master worker scheme



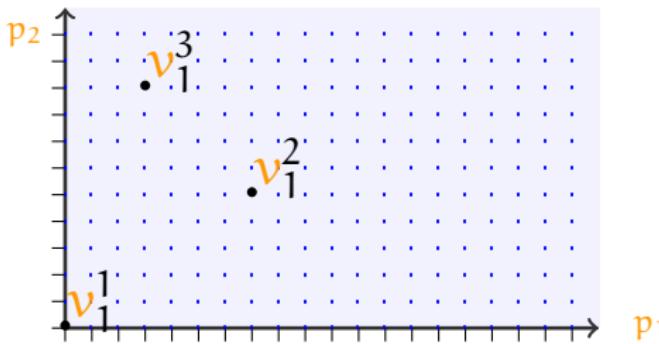
Master-worker distribution scheme:

- **Workers:** ask the master for a point (integer parameter valuation), calls PRP on that point, and send the result (constraint) to the master
- **Master:** is responsible for smart repartition of data between the workers
  - Not trivial at all

# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

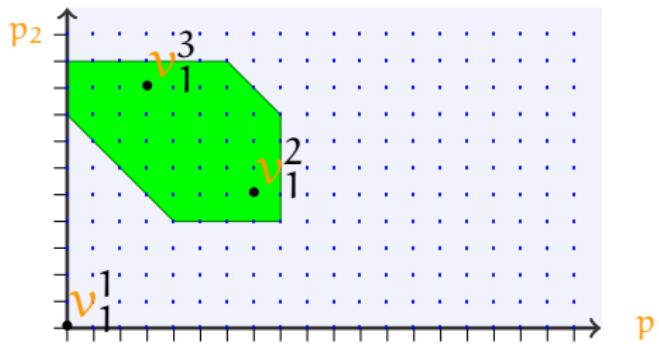
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

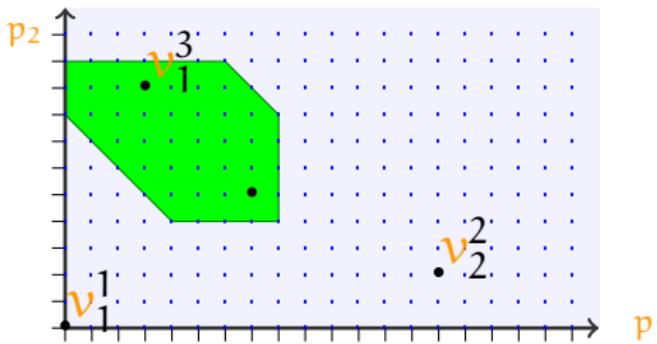
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

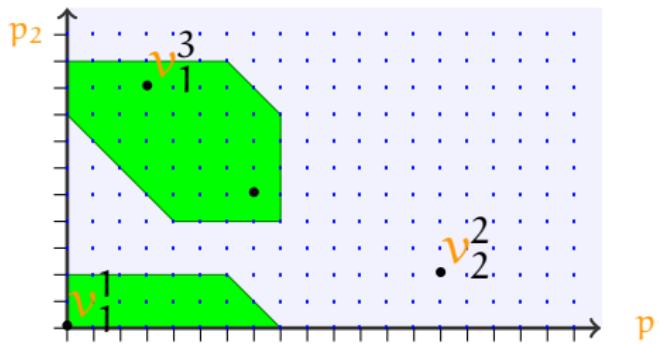
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

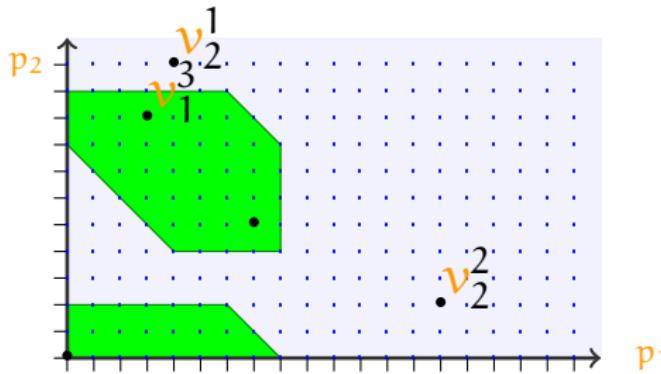
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

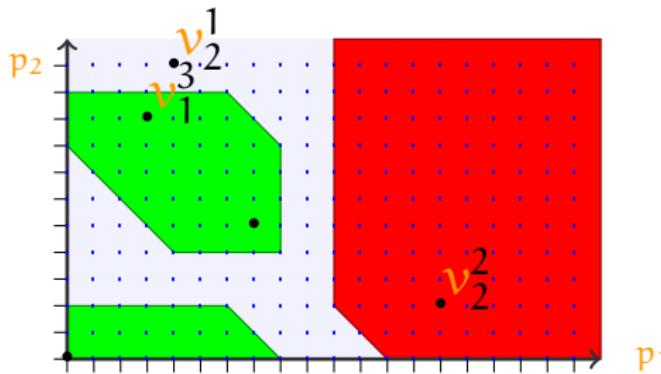
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

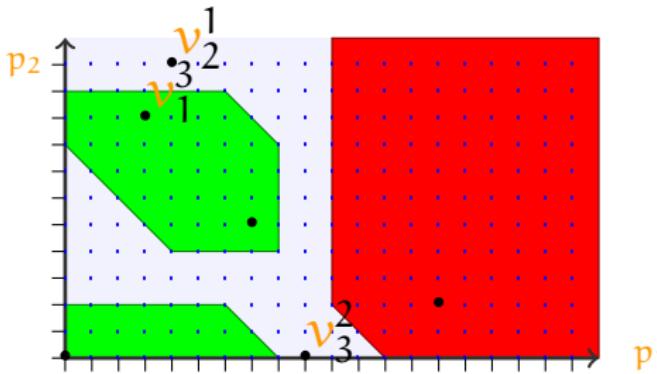
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

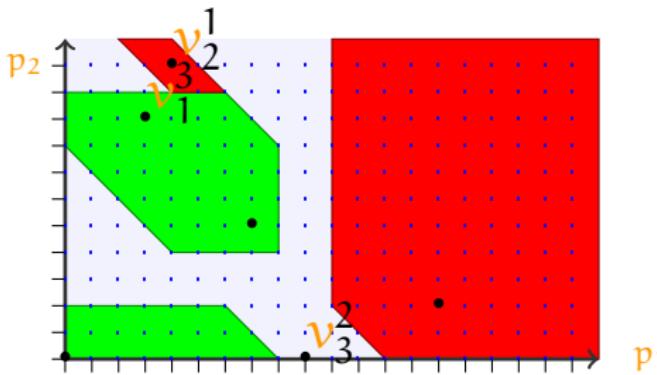
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

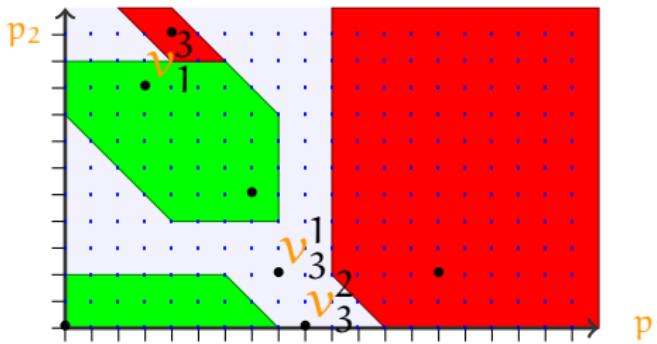
- 1 master
- 3 workers



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Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

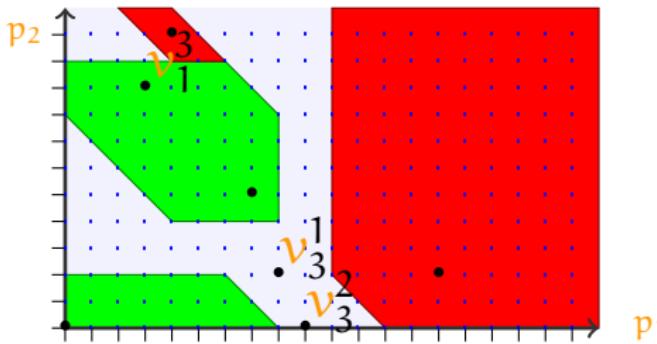
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Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

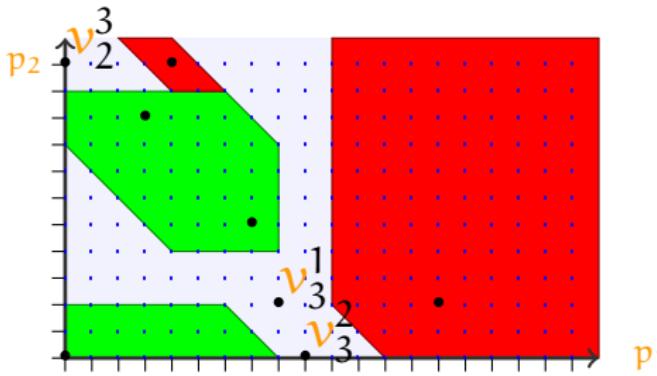
- 1 master
- 3 workers



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Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

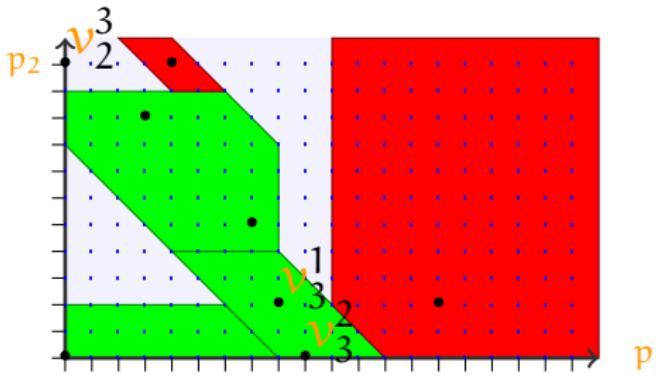
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

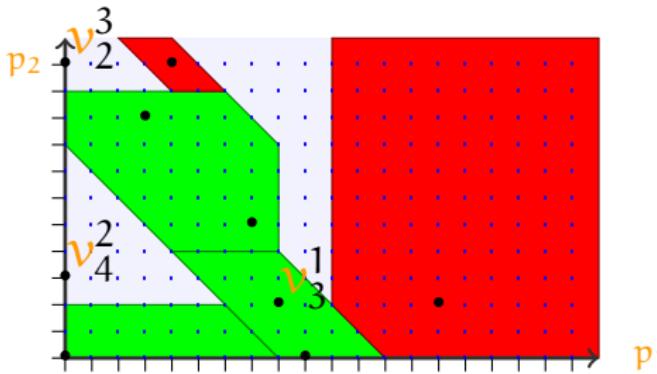
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

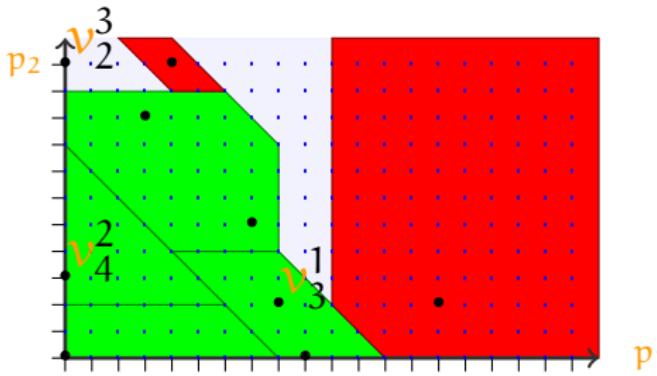
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

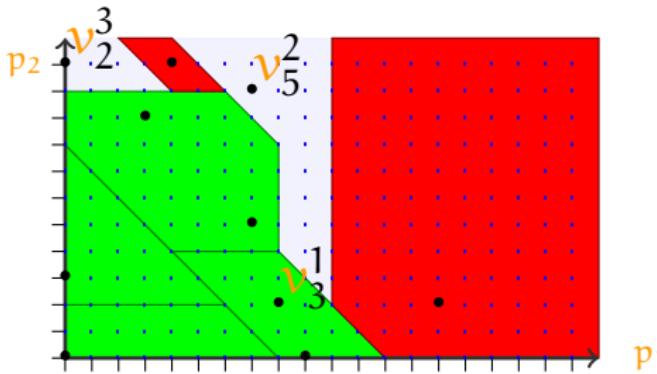
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

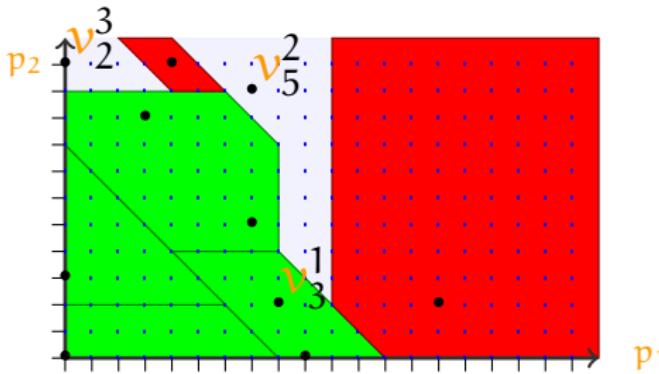
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

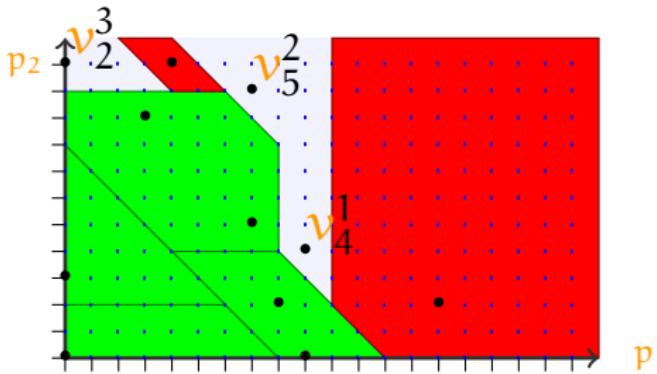
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

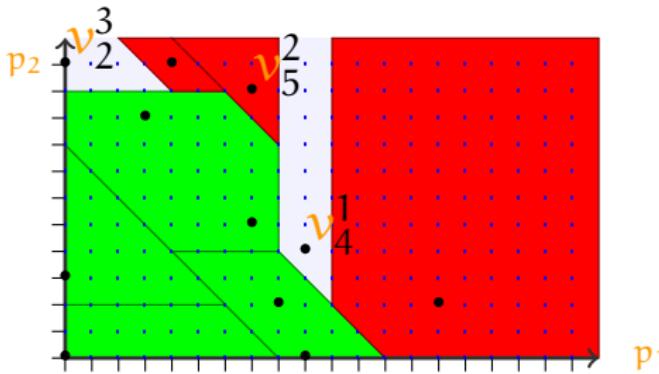
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

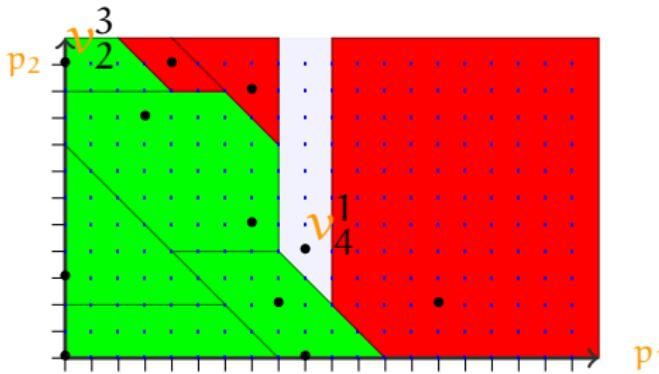
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

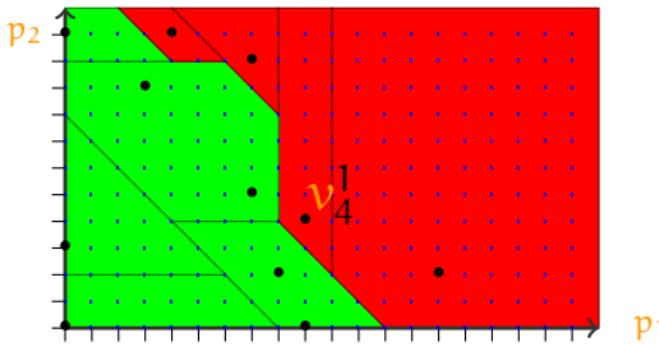
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

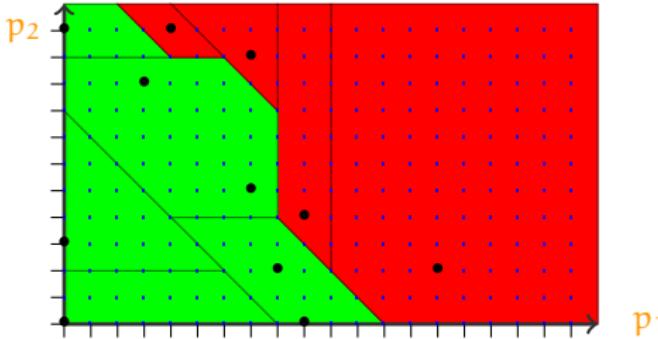
- 1 master
- 3 workers



# Distributing PRPC: general scheme

Example with 2 parameters ( $p_1$  and  $p_2$ ) and 4 nodes:

- 1 master
- 3 workers



Problem:

- redundant computations

# Dynamic domain decomposition

Most efficient distributed algorithm (so far!):

“Domain decomposition” scheme

[A., Coti, Nguyen 2015]

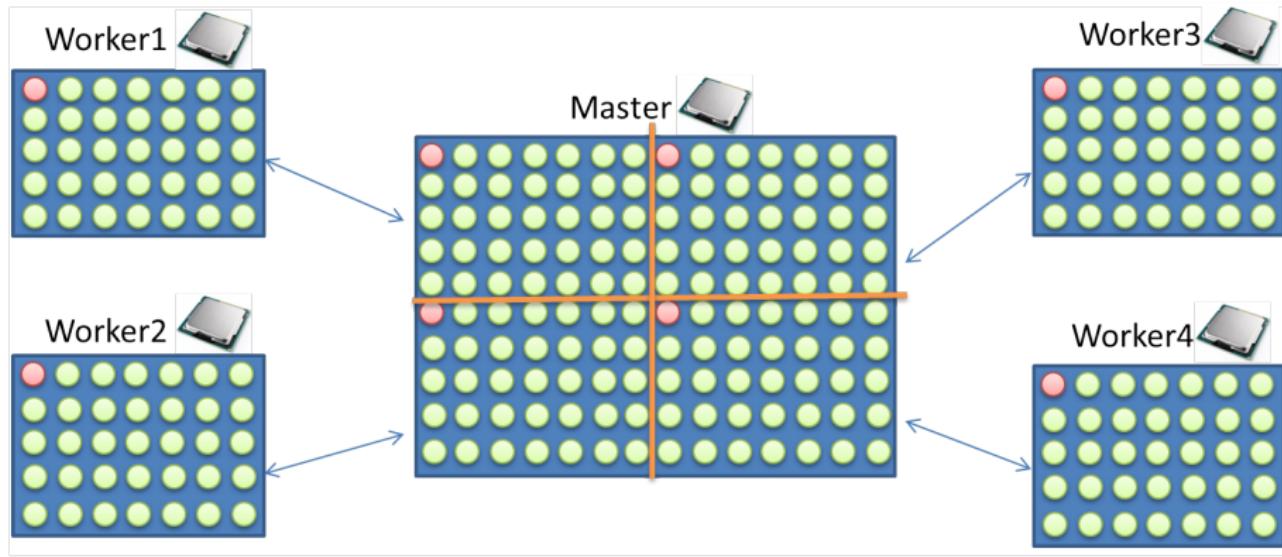
## ■ Master

- 1 initially splits the parameter domain into **subdomains** and send them to the workers
- 2 when a worker has completed its subdomain, the master splits another subdomain, and sends it to the idle worker

## ■ Workers

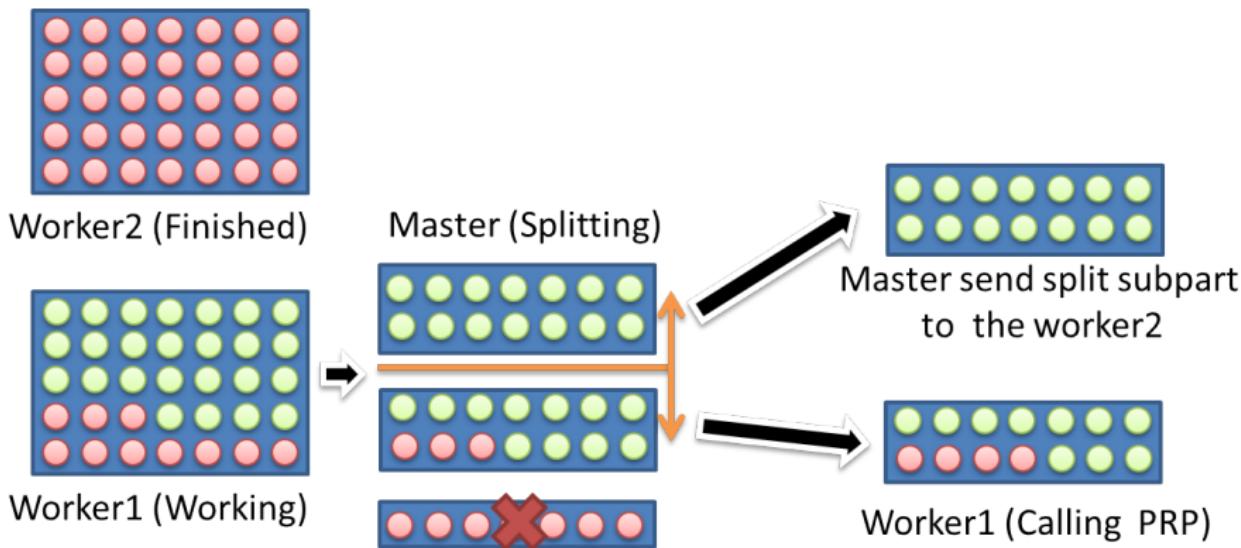
- 1 receive the subdomain from the master
- 2 call PRP on the points of this subdomain
- 3 send the results (list of constraints) back to the master
- 4 ask for more work

# Domain decomposition: Initial splitting



- Prevent choosing close points
- Prevent bottleneck phenomenon at the master's side
  - Master only responsible for gathering constraints and splitting subdomains

# Domain decomposition: Dynamic splitting



- Master can **balance workload** between workers

# Implementation in IMITATOR

Implemented in IMITATOR using the MPI paradigm (message passing interface)

Distributed version up to 44 times faster using 128 nodes than the monolithic EFsynth

[André et al., 2015a]

# Outline

- 1 Parametric Timed Automata
- 2 Modeling and Verifying Real-Time Systems
- 3 Verifying a Real-time System under Uncertainty
- 4 Distributed Verification of Distributed Systems
- 5 Conclusion and Perspectives

# Summary

- Parametric timed automata: a powerful (though undecidable) formalism to model and verify real-time systems
  - with preemption
  - with unknown or uncertain periods, jitters or WCETs

# Perspectives

Address harder problems

- Thales challenge: what is the **minimum time between two lost frames**? (due to the uncertain periods)
  - Requires to model check **thousands of frame processings**

Improve the efficiency of parameter synthesis techniques

- Promising heuristics: approximations using the integer hull  
[Jovanović et al., 2015, André et al., 2015b]
- Distributed parameter synthesis
  - Multi-core synthesis [Laarman et al., 2013]
  - Distributed synthesis based on locations [Zhang et al., 2016]

# And to finish...

## Advertisement

Interested in the domain of verification with parameters?

We have **post-doc positions** in Nantes, Paris 7 and Paris 13!

Starting anytime.



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157–173. Springer.

## Additional explanation

# Explanation for the 4 pictures in the beginning



Allusion to the Northeast blackout (USA, 2003)

Computer bug

Consequences: 11 fatalities, huge cost

(Picture actually from the Sandy Hurricane, 2012)



Error screen on the earliest versions of Macintosh



Allusion to the sinking of the Sleipner A offshore platform (Norway, 1991)

No fatalities

Computer bug: inaccurate finite element analysis modeling

(Picture actually from the Deepwater Horizon Offshore Drilling Platform)



Allusion to the MIM-104 Patriot Missile Failure (Iraq, 1991)

28 fatalities, hundreds of injured

Computer bug: software error (clock drift)

(Picture of an actual MIM-104 Patriot Missile, though not the one of 1991)

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Title: Hurricane Sandy Blackout New York Skyline

Author: David Shankbone

Source: [https://commons.wikimedia.org/wiki/File:Hurricane\\_Sandy\\_Blackout\\_New\\_York\\_Skyline.JPG](https://commons.wikimedia.org/wiki/File:Hurricane_Sandy_Blackout_New_York_Skyline.JPG)

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Author: Przemub

Source: [https://commons.wikimedia.org/wiki/File:Sad\\_mac.png](https://commons.wikimedia.org/wiki/File:Sad_mac.png)

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Title: Deepwater Horizon Offshore Drilling Platform on Fire

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## Source of the graphics used II



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Author: LadyofHats

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Title: Smiley green alien big eyes (cry)

Author: LadyofHats

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Author: Citron

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